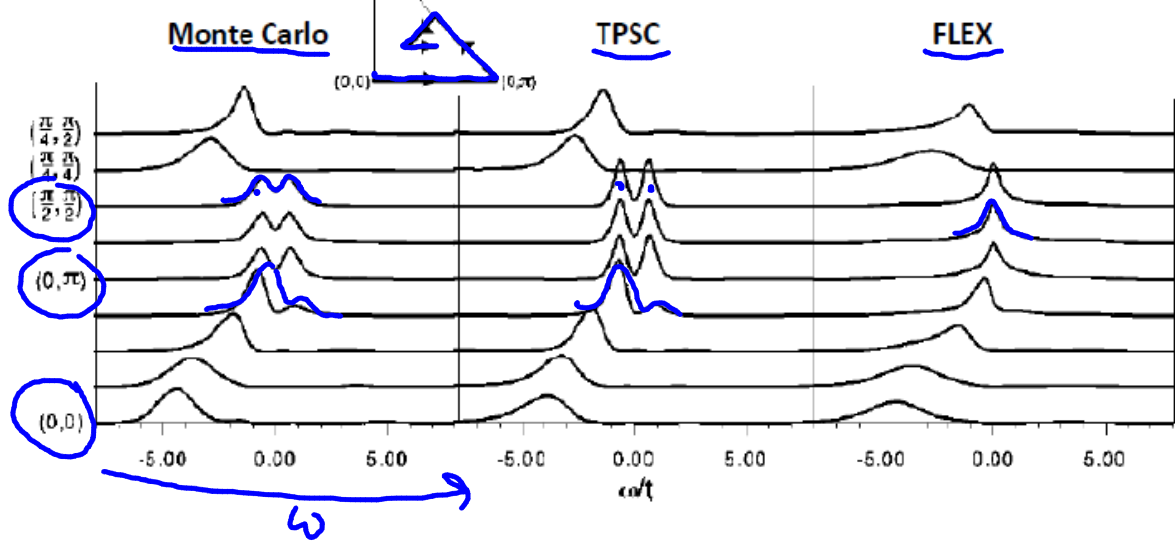


$T = 0.2t$

$A(k, \omega)$

$n=1$
 $\beta=5$



- 46.3 Hartree-Fock + RPA ✓
- 46.4 RPA et principe de Pauli ✓
- 46.5 RPA transition de phase et Mermin-Wagner ✓
- 47. Approche Auto-Cohérente à deux particules ACDP-TPSC
 - 47.1 Étape 1. Modes collectifs, auto-cohérence à 2 particules
 - 47.2 Étape 2. Meilleure self-énergie
 - 47.3 Test de précision - Cohérence 1 et 2 particules

48. TPSC test de précision, aspects physiques ✓

48.1 Approche physique, spin et charge ✓

48.2 Mermin-Wagner, Kanamori-Bruceker ✓

48.3 Comparaisons

1. Spin-charge ✓

2. Self ✓

48.4 Pseudogap ?

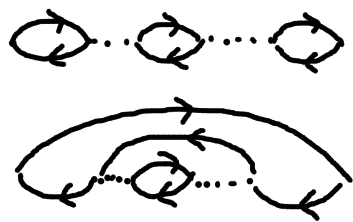
49. Théorie de champ moyen dynamique DMFT ✓

49.1 Impuretés quantiques



$$U = 0$$

$$\epsilon_h = -2t (\cos h_x + \cos h_z)$$



$$\left. \begin{array}{l} \epsilon_h^{\max} = 4t \\ \epsilon_h^{\min} = -4t \end{array} \right\} W = 8t$$

46.3 H.F. + RPA

$$\frac{\delta \mathcal{H}}{\delta \varphi} = \mathcal{H} \varphi + \mathcal{H} \left(\frac{\delta \mathcal{H}}{\delta \mathcal{H}} \frac{\delta \mathcal{H}}{\delta \varphi} \right) \varphi$$

$$\chi_{ch}(1,2) = - \sum_{\sigma\sigma'} \frac{\delta \mathcal{H}_\sigma(1,1')}{\delta \varphi_{\sigma'}(2,2')} = -2 \mathcal{H}(1,2) \mathcal{H}(2,1)$$

$$- \mathcal{H}(1,3) \left(\frac{\delta \mathcal{H}_\uparrow(3,4)}{\delta \mathcal{H}_\uparrow(6,7)} + \frac{\delta \mathcal{H}_\uparrow(3,4)}{\delta \mathcal{H}_\downarrow(6,7)} \right) \sum_{\sigma\sigma'} \frac{\delta \mathcal{H}_\sigma(6,7)}{\delta \varphi_{\sigma'}(2,2')}$$

Calcul des pages suivantes χ_0

$$\chi_{ch}(1,2) = -2 \mathcal{H}(1,2) \mathcal{H}(2,1) + \mathcal{H}(1,3) \mathcal{H}(3,1) \cup \chi_{ch}(3,2)$$



$$\chi_{ch}(q) = \chi_0(q) - \frac{U}{2} \chi_0(q) \chi_{ch}(q)$$

$$\chi_{ch}^{SP}(q) = \frac{\chi_0(q)}{1 \pm \frac{U}{2} \chi_0(q)}$$

$$\begin{aligned} \Sigma_{\sigma}(1, \bar{1}) \mathcal{H}_{\sigma}(\bar{1}, 2) &= -v \langle T_{\sigma} \psi_{\sigma}^{\dagger}(\bar{1}) \psi_{\sigma}(1) \psi_{\sigma}(1) \psi_{\sigma}^{\dagger}(2) \rangle \\ &= -v \left[\frac{\delta \mathcal{H}_{\sigma}(1, 2)}{\delta \psi_{\sigma}(1^{\dagger}, 1)} - \mathcal{H}_{\sigma}(1, 1^{\dagger}) \mathcal{H}_{\sigma}(1, 2) \right] \end{aligned}$$

$$\begin{aligned} \mathcal{H}_{\sigma}^{-1} &= \mathcal{H}_{\sigma}^{-1} - \varphi - \Sigma_{\sigma} \\ &\quad \uparrow \quad \uparrow \\ \mathcal{H}_{\sigma} &+ \mathcal{H}_{\sigma} \frac{\delta \Sigma_{\sigma}}{\delta \varphi} \mathcal{H}_{\sigma} \\ \frac{\delta \mathcal{H}_{\sigma}}{\delta \varphi} \mathcal{H}_{\sigma}^{-1} + \mathcal{H}_{\sigma} \frac{\delta \mathcal{H}_{\sigma}^{-1}}{\delta \varphi} &= 0 \end{aligned}$$

$$\left[\sum_{\sigma} (1, i)_{\sigma} \mathcal{Y}_{\sigma}(\bar{1}, \bar{2})_{\sigma} = U \mathcal{Y}_{\sigma}(1, 1^+)_{\sigma} \mathcal{Y}_{\sigma}(1, \bar{2})_{\sigma} \right] \mathcal{Y}_{\sigma}^{-1}(\bar{2}, 3)$$

$$\sum_{\sigma} (1, 3)_{\sigma} = U \mathcal{Y}_{\sigma}(1, 1^+)_{\sigma} \delta(1-3)$$

$$\left[\frac{\delta \sum_{\sigma} (1, 3)}{\delta \mathcal{Y}_{\sigma}(4, 5)} = \delta(1-3) \cup \delta(1-4) \delta(1^+-5) \quad \frac{\delta \sum_{\sigma}}{\delta \mathcal{Y}_{\sigma}} = 0 \right.$$

$$\left. \rightarrow U_{\sigma} \delta(1-3) \delta(1-4) = U \delta(1-3) \delta(1-4) \delta(1^+-5) \right.$$

46.4 RPA et principe de Pauli

$$\begin{aligned}
 \chi_{ch}(1,1) &= \langle n(1)n(1) \rangle - \langle n(1) \rangle^2 \\
 &= \langle (n_\uparrow + n_\downarrow)(n_\uparrow + n_\downarrow) \rangle - n^2 \\
 &= \langle n_\uparrow^2 \rangle + \langle n_\downarrow^2 \rangle + 2\langle n_\uparrow n_\downarrow \rangle - n^2 \\
 &= n + 2\langle n_\uparrow n_\downarrow \rangle - n^2 \quad \leftarrow
 \end{aligned}$$

$$\chi_{sp}(1,1) = \langle (n_\uparrow - n_\downarrow)(n_\uparrow - n_\downarrow) \rangle = n - 2\langle n_\uparrow n_\downarrow \rangle \quad \leftarrow$$

$$\boxed{\chi_{ch}(1,1) + \chi_{sp}(1,1) = 2n - n^2} \quad \text{indép. de } U$$

$$\frac{T}{N} \sum_{\vec{q}} \sum_{q_n} e^{i\vec{q} \cdot (\vec{r}_i - \vec{r}_j) - iq_n (\tau_i - \tau_j)} \chi(\vec{q}, iq_n)$$

$$= \chi(\tau_i, \tau_j; \tau_j, \tau_i)$$

$$\boxed{\frac{T}{N} \sum_{\vec{q}} (\chi_{ch} + \chi_{sp}) = 2n - n^2}$$

$$\frac{T}{N} \sum_{\vec{q}} \left(\frac{\chi_0}{1 + \frac{U}{2}\chi_0} + \frac{\chi_0}{1 - \frac{U}{2}\chi_0} \right) = 2n - n^2$$

$$\begin{aligned}
 \chi_0(\vec{q}) &= \int \frac{d\omega}{\pi} \frac{\chi''(\omega)}{iq_n - \omega} \\
 &= \int \frac{d\omega}{\pi} \frac{\omega \chi''(\omega)}{q_n^2 + \omega^2}
 \end{aligned}$$

46.5 Transitions de phase et Mermin-Wagner

$$\chi_{sp}(\vec{q}) = \frac{\chi_0(\vec{q})}{1 - \frac{v}{2} \chi_0(\vec{q})}$$

$$\chi_{sp}(\vec{q}, 0) \rightarrow \infty$$

Cas particulier

$$E_k = -2t(\cos k_x + \cos k_y + \cos k_z)$$

Demi-rempli: $\mu = 0$

$$\chi_0(\vec{q}) = -2 \sum_k \frac{f(\epsilon_k) - f(\epsilon_{k+\vec{q}})}{\epsilon_k - \epsilon_{k+\vec{q}}}$$

Soit

$$\vec{q} = Q = (\pi, \pi, \pi)$$

$$\chi_0(Q) = -2 \sum_k \frac{2f(\epsilon_k) - 1}{2\epsilon_k}$$

$$\epsilon_{k+Q} = -\epsilon_k$$

$$f(-\epsilon_k) = 1 - f(\epsilon_k)$$

$$\frac{1}{e^{-\beta\epsilon_k} + 1} = 1 - \frac{1}{e^{\beta\epsilon_k} + 1}$$

$$= +2 \sum_k \frac{\tanh(\beta\epsilon_k/2)}{2\epsilon_k}$$

$$= \int_{-\infty}^{\infty} d\epsilon N(\epsilon) \frac{\tanh(\beta\epsilon/2)}{2\epsilon} \sim 2N(0) \int_0^{\infty} \frac{\tanh \frac{\beta\epsilon}{2}}{2\epsilon} d\epsilon$$

$$\sim 2N(0) \int_T^{\infty} \frac{1}{2\epsilon} d\epsilon + \dots$$

$$\sim 2N(0) \ln \frac{\infty}{T}$$

$$1 - \frac{v}{2} 2N(0) \ln \frac{\infty}{T} = 0$$

47. ACDP - TPSC

47.1 Etape 1

$$\sum_{\sigma} \psi_{\sigma}(1, \bar{1})_{\sigma} \psi_{\sigma}(\bar{1}, 2)_{\sigma} = -U \langle T_{\sigma} \psi_{\sigma}^{\dagger}(1) \psi_{\sigma}(1) \psi_{\sigma}(1) \psi_{\sigma}^{\dagger}(2) \rangle$$

impose \rightarrow $\sum_{\sigma} \psi_{\sigma}(1, \bar{1})_{\sigma} \psi_{\sigma}(\bar{1}, 1^{+})_{\sigma} = U \langle n_{\downarrow} n_{\uparrow} \rangle_{\sigma}$ $\langle n_{\uparrow} n_{\downarrow} \rangle = \langle n_{\uparrow} \rangle$

$$\sum_{\sigma} \psi_{\sigma}(1, \bar{1})_{\sigma} \psi_{\sigma}(\bar{1}, 2)_{\sigma} = A_{\sigma} \psi_{\sigma}(1, 1^{+})_{\sigma} \psi_{\sigma}(1, 2)_{\sigma}$$

$$U \langle n_{\uparrow} n_{\downarrow} \rangle_{\sigma} = A_{\sigma} \langle n_{\downarrow} \rangle_{\sigma} \langle n_{\uparrow} \rangle_{\sigma}$$

$$A_{\sigma} = \frac{U \langle n_{\uparrow} n_{\downarrow} \rangle_{\sigma}}{\langle n_{\uparrow} \rangle_{\sigma} \langle n_{\downarrow} \rangle_{\sigma}} \quad \text{(HF)}$$

$$\sum_{\sigma}^{\text{HF}} \psi_{\sigma}(1, 3) = U \delta(1-3) \psi_{\sigma}(1, 1^{+})$$

$$\sum_{\sigma}^{\text{TPSC}} \psi_{\sigma}(1, 3) = \frac{U \langle n_{\uparrow} n_{\downarrow} \rangle_{\sigma}}{\langle n_{\uparrow} \rangle_{\sigma} \langle n_{\downarrow} \rangle_{\sigma}} \psi_{\sigma}(1, 1^{+}) \delta(1-3)$$

$$U_{sp} \rightarrow \frac{\delta \sum_{\uparrow}}{\delta \psi_{\downarrow}} - \frac{\delta \sum_{\uparrow}}{\delta \psi_{\uparrow}}$$

$$U_{sp} = \frac{U \langle n_{\uparrow} n_{\downarrow} \rangle}{\langle n_{\uparrow} \rangle \langle n_{\downarrow} \rangle}$$

U_{ch}


$$\frac{T}{N} \sum_{\mathbf{q}} \chi_{sp} = \frac{T}{N} \sum_{\mathbf{q}} \frac{\chi_0(\mathbf{q})}{1 - \frac{U_{sp}}{2} \chi_0(\mathbf{q})} = n - 2 \langle n_{\uparrow} n_{\downarrow} \rangle$$

$$\frac{T}{N} \sum_{\mathbf{q}} \frac{\chi_0(\mathbf{q})}{1 + \frac{U_{ch}}{2} \chi_0(\mathbf{q})} = n + 2 \langle n_{\uparrow} n_{\downarrow} \rangle - n^2$$

$$\chi_{ch}(q=0, \omega \neq 0) = 0 \quad \langle N(t)N(0) \rangle$$

↑ Conservation
↑ → $\delta(\omega)$

47.2 Etape 2

Gas d'électrons 

$$\begin{aligned} \Sigma^{(1)}(1,2) &= -U \left[\frac{\delta \mathcal{H}_\sigma(1,\bar{2})}{\delta \varphi_\sigma(1^+,1)} - \mathcal{H}_\sigma(1,1^+) \mathcal{H}_\sigma(1,\bar{2}) \right] \mathcal{H}_\sigma^{-1}(\bar{2},2) \\ &= U \mathcal{H}_\sigma(1,1^+) \delta(1-\bar{2}) - U \frac{\delta \mathcal{H}_\sigma(1,\bar{2})}{\delta \varphi_\sigma(1^+,1)} \mathcal{H}_\sigma^{-1}(\bar{2},2) \end{aligned}$$

$$\frac{\delta \mathcal{H}_\sigma}{\delta \varphi_\sigma} \mathcal{H}_\sigma^{-1} = -\mathcal{H}_\sigma \frac{\delta \mathcal{H}_\sigma^{-1}}{\delta \varphi_\sigma} \quad \mathcal{H}_\sigma^{-1} = \mathcal{H}_\sigma^{-1} - \varphi - \Sigma$$

$$= +\mathcal{H}_\sigma \frac{\delta \Sigma_\sigma}{\delta \mathcal{H}_\sigma} \frac{\delta \mathcal{H}_\sigma^{-1}}{\delta \varphi_\sigma}$$



$$\Sigma^{(2)}(k) = U n_\sigma + \frac{T}{N} \frac{U}{g} \sum_{\mathcal{G}} \left[U_{sp} \chi_{sp}^{(1)}(\mathcal{G}) + U_{ch} \chi_{ch}^{(1)}(\mathcal{G}) \right] \mathcal{H}_\sigma^{-1}(k+\mathcal{G})$$

$$\Sigma(1,\bar{1}) \mathcal{H}(\bar{1},1^+) = U \langle n_p n_\sigma \rangle$$

$$\frac{T}{N} \sum_k \Sigma^{(2)}(k) \mathcal{H}^{(1)}(k) e^{-ik \cdot 0} = U \langle n_p n_\sigma \rangle$$

