Doping evolution of the superconducting gap structure in the underdoped iron arsenide Ba$_{1-x}$K$_x$Fe$_2$As$_2$ revealed by thermal conductivity

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The thermal conductivity $\kappa$ of the iron-arsenide superconductor Ba$_{1-x}$K$_x$Fe$_2$As$_2$ was measured for heat currents parallel and perpendicular to the tetragonal $c$ axis at temperatures down to 50 mK and in magnetic fields up to 15 T. Measurements were performed on samples with compositions ranging from optimal doping ($x = 0.34$, $T_c = 39$ K) down to dopings deep into the region where antiferromagnetic order coexists with superconductivity ($x = 0.16$, $T_c = 7$ K). In zero field, there is no residual linear term in $\kappa(T) = 0$ at any doping, whether for in-plane or interplane transport. This shows that there are no nodes in the superconducting gap. However, as $x$ decreases into the range of coexistence with antiferromagnetism, the residual linear term grows more and more rapidly with applied magnetic field. This shows that the superconducting energy gap develops minima at certain locations on the Fermi surface and these minima deepen with decreasing $x$. We propose that the minima in the gap structure arise when the Fermi surface of Ba$_{1-x}$K$_x$Fe$_2$As$_2$ is reconstructed by the antiferromagnetic order.

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I. INTRODUCTION

Soon after the discovery of superconductivity in iron-based materials [1], it was recognized that a conventional phonon-mediated pairing cannot account for the high critical temperature $T_c$ [2]. The observation of superconductivity in proximity to a magnetic quantum critical point [3] points instead to magnetically mediated pairing [4], a scenario also discussed for cuprate and heavy-fermion materials [5]. Because such pairing is based on a repulsive interaction, it implies that the superconducting order parameter must change sign around the Fermi surface [6]. This is the case for the $d$-wave state realized in cuprate superconductors, where the gap has symmetry-imposed nodes where the Fermi surface crosses the diagonals at $k_x = k_y$. In the $s_{\pm}$ state proposed for iron-based superconductors [7], there are no symmetry-imposed nodes, but the order parameter has a different sign on the hole and electron pockets. One can see that in order to identify the pairing symmetry, associated with a particular pairing mechanism, it is important to determine the anisotropy of the gap structure.

In the iron-based superconductors, the superconducting gap structure has been studied most extensively in the oxygen-free materials with BaFe$_2$As$_2$ (Ba122) as a parent compound [8]. High-quality single crystals can be grown with various types of dopants to induce superconductivity in the parent antiferromagnet, including hole doping with potassium in Ba$_{1-x}$K$_x$Fe$_2$As$_2$ (K-Ba122) [9], electron doping with cobalt in Ba(Fe$_{1-y}$Co$_y$)$_2$As$_2$ (Co-Ba122) [10, 11], and iso-electron substitution of arsenic with phosphorus in BaFe$_2$(As$_{1-x}$P$_x$)$_2$ (P-Ba122) [12].

Early on, an angle-resolved photoemission spectroscopy study of optimally doped K-Ba122 found a full superconducting gap on all sheets of the Fermi surface [13]. This was explained within the $s_{\pm}$ scenario [14]. However, subsequent studies of the superconducting gap structure in Ba122 revealed considerable diversity. In P-Ba122, the gap is nodal for all dopings [15, 16]. In Co-Ba122, the gap is isotropic at optimal doping but it develops nodes in both under- and overdoped compositions [17–21]. In K-Ba122, the gap is also isotropic at optimal doping [13, 22], but it develops some $k$ dependence with decreasing $x$ [23–26], and there are nodes in the gap at $x = 1.0$ (KFe$_2$As$_2$) [27–32], where the pairing symmetry may in fact be $d$ wave [22, 30, 33].

This diversity in the gap structure has been attributed in part to a competition between intraband and interband pairing interactions [34, 35]. Another factor that can affect the gap structure is the presence of a coexisting antiferromagnetic order [36]. The importance of the coexisting magnetism for the superconducting gap structure of hole-doped K-Ba122 was suggested by a previous penetration depth study [25], which found a rapid loss of superfluid response on underdoping into the coexistence range. A similar decrease was observed in electron-doped Co-122 [37]. In this paper, we report a study of the superconducting gap structure in K-Ba122 using directional heat transport measurements, for concentrations that cross into the region of the phase diagram where superconductivity and antiferromagnetism coexist. We observe that the gap, which is isotropic just above the coexistence region, gradually develops $k$ dependence as the magnetic order grows, with minima that deepen with decreasing $x$. We attribute these minima to the reconstruction of the Fermi surface caused by the antiferromagnetic order.
Our main findings may be summarized as follows. The superconducting gap of K-Ba122 does not have nodes for a broad range of underdoped compositions in the phase diagram, from $x = 0.16$ ($T_c = 7$ K) to $x = 0.34$ ($T_c = 39$ K). However, a notable modulation of the superconducting gap magnitude develops in the coexistence regime of superconductivity and magnetism ($x < 0.25$), as found in a strongly enhanced response to the application of a magnetic field. The $a - c$ anisotropy of heat transport in the superconducting state of K-Ba122 is identical to the anisotropy of the normal state, suggesting that the modulation of the superconducting energy gap is predominantly in the conducting plane, in contrast to the electron-doped Co-Ba122 [20].

II. METHODS

Single crystals of Ba$_{1-x}$K$_x$Fe$_2$As$_2$ were grown using a self-flux technique [9]. Nine samples were cut for $a$-axis transport and seven for $c$-axis transport. The samples are labeled by their $T_c$ value. Details of the sample preparation, screening, compositional analysis, and resistivity measurements can be found in Ref. [38]. The technique for making contacts is described in Refs. [39,40]. The superconducting $T_c$ of underdoped samples changes monotonically with $x$. We find that the relation between $T_c$ and $x$ is well described by the formula $T_c = 38.5 - 54(0.345 - x) - 690(0.345 - x)^2$. The thermal conductivity was measured in a standard one-heater two-thermometer technique, described elsewhere [20], for two directions of the heat flow: parallel ($J || c$; $\kappa_c$) and perpendicular ($J || a$; $\kappa_a$) to the [001] tetragonal $c$ axis. The magnetic field $H$ was applied along the $c$ axis. Measurements were done on warming after cooling from above $T_c$ in a constant field, to ensure a homogeneous field distribution in the sample.

At least two samples were measured for all compositions to ensure reproducibility. Resistivity measurements to determine the upper critical field were performed in a Quantum Design physical property measurement system down to 1.8 K.

III. RESULTS

A. Electrical resistivity

In the right panels of Fig. 1, the resistivity of four K-Ba122 samples, normalized to its value at $T = 300$ K, is plotted as a function of temperature, for both $J || a$ and $J || c$. The values at 300 K, $\rho(300)$, do not change much with doping, and $\rho(300) \approx 300$ and 1000–2000 $\mu$cm, respectively [38,41]. We use the resistivity curves of each sample to determine $T_c$ and the residual resistivity $\rho_0$, obtained from a smooth extrapolation of $\rho(T)$ to $T = 0$ (see Fig. 1). We use $\rho_0$ to estimate the residual value of the thermal conductivity in the normal state, $\kappa_N/T$, via the Wiedemann-Franz law, $\kappa_N/T = L_0/\rho_0$, where $L_0 \equiv (\pi^2/3)(k_B/e)^2$.

B. Thermal conductivity

The thermal conductivity of the same four samples, measured using the same contacts, is also displayed in Fig. 1. The data in the top row are for a heat current along the $a$ axis, giving $\kappa_a$, while the data in the bottom panels are for the interplane heat current, giving $\kappa_c$. The fits show that the data below 0.3 K are well described by the power-law function $\kappa/T = a + bT^\alpha$. The first term, $a \equiv \kappa_0/T_c$, is the residual linear term, entirely due to electronic excitations [42]. The second term is due to phonons, which at low temperatures are scattered by the sample boundaries, with $1 < \alpha < 2$ [43,44]. We see that, for $H = 0$, $\kappa_0/T = 0$ for all samples, within error.
bars. At the highest doping ($T_c = 37 - 38$ K), $\kappa_0/T$ remains negligible even when a magnetic field of 15 T is applied. At lower K concentration, however, $\kappa_0/T$ increases significantly upon application of a magnetic field. Our current data are consistent with our previous measurement of $\kappa_0$ in a K-Ba122 sample with $T_c = 26$ K [23].

Figure 2 shows how the residual linear term $\kappa_0/T$, normalized by the normal-state conductivity, $\kappa_0/T$, as a function of magnetic field $H$, normalized by the upper critical field $H_c$ (defined in Fig. 3). The data for in-plane ($J||a$, open symbols) and interplane ($J||c$, closed symbols) transport are shown for five K concentrations, indicated by their $T_c$ values. For comparison, we reproduce corresponding data for the isotropic $s$-wave superconductor Nb [42,45], the multiband $s$-wave superconductor NbSe$_2$ [46], and the nodal $d$-wave superconductor Tl-2201 [47].

**FIG. 2.** Residual linear term $\kappa_0/T$, normalized by the normal-state conductivity, $\kappa_0/T$, as a function of magnetic field $H$, normalized by the upper critical field $H_c$ (defined in Fig. 3). The data for in-plane ($J||a$, open symbols) and interplane ($J||c$, closed symbols) transport are shown for five K concentrations, indicated by their $T_c$ values. For comparison, we reproduce corresponding data for the isotropic $s$-wave superconductor Nb [42,45], the multiband $s$-wave superconductor NbSe$_2$ [46], and the nodal $d$-wave superconductor Tl-2201 [47].

In the left panel of Fig. 3, we plot the upper critical field $H_c$ as a function of temperature, for four samples, with $T_c = 7$ (blue), 10 (magenta), 12 (green), and 19 K (black). $H_c$ is determined from electrical resistivity measurements [41]. The blue square shows the $H_c$ value determined from thermal conductivity measurements on the $T_c = 7$ K sample. The lines are a linear fit of each data set, extrapolated to $T = 0$. The value of $H_c$ thus extrapolated to $T = 0$, $H_c(0) = H_c$, is plotted vs $x$ in the right panel. Right panel: $H_c(0)$ vs $T_c$ from data in the left panel (red dots), plus one point at high doping from published data (black diamond) [41]. The line is a polynomial fit of the data, used to extract the values of $H_c$ for the samples $T_c$ between 7 and 25 K.

**FIG. 3.** Left panel: Upper critical field $H_c(T)$ for $H||c$, as a function of temperature, for four samples, with $T_c = 7$ (blue), 10 (magenta), 12 (green), and 19 K (black). $H_c$ is determined from electrical resistivity measurements [41]. The blue square shows the $H_c$ value determined from thermal conductivity measurements on the $T_c = 7$ K sample. The lines are a linear fit of each data set, extrapolated to $T = 0$. The value of $H_c$ thus extrapolated to $T = 0$, $H_c(0) = H_c$, is plotted vs $x$ in the right panel. Right panel: $H_c(0)$ vs $T_c$ from data in the left panel (red dots), plus one point at high doping from published data (black diamond) [41]. The line is a polynomial fit of the data, used to extract the values of $H_c$ for the samples $T_c$ between 7 and 25 K.

**C. Upper critical field**

In the left panel of Fig. 3, we plot the upper critical field $H_c$ as a function of temperature, for four values of $x$, as determined from resistivity measurements for $H||c$. For the sample at $x = 0.16$ ($T_c = 7$ K), a field of 15 T is sufficient to reach the normal state. Using the fact that $\kappa_0/T$ saturates above $H \approx 9$ T in that sample, we estimate that $H_c \approx 9$ T at $T \rightarrow 0$. We see that this value agrees with a linear extrapolation of the resistively determined $H_c(T)$. For the other dopings, we obtain $H_c(0)$, the value of $H_c(T)$ at $T \rightarrow 0$, by linear extrapolation. Note that the slope of the $H_c(T)$ curve increases with increasing $T_c$, as expected for superconductors in the clean limit [41], which holds for K-Ba122 at all dopings. In the right panel of Fig. 3, we plot $H_c(0)$ versus $T_c$, including published data from a sample with a slightly higher concentration [41].

**IV. DISCUSSION**

From Fig. 2, three main characteristics of the gap structure of K-Ba122 can be deduced. First, the fact that in zero field $\kappa_0/T = 0$ at all dopings, for both current directions, immediately implies that there are no zero-energy quasiparticles at $H = 0$. From this we can infer that there are no nodes in the superconducting gap anywhere on the Fermi surface.

Secondly, we see that the rate at which a magnetic field excites heat-carrying quasiparticles in K-Ba122 varies enormously with doping. In the absence of nodes, quasiparticle conduction proceeds by tunneling between states localized in the cores of adjacent vortices, which grows exponentially as the intervortex separation decreases with increasing field [45], as observed in a superconductor with an isotropic gap like Nb (see Fig. 2). The exponential rate is controlled by the coherence length, which is inversely proportional to the gap magnitude. If the gap is large everywhere on the Fermi surface, the coherence length will be small everywhere, and the growth of $\kappa_0/\kappa_N$ versus $H$ will be very slow at low $H/H_c$. This is what we observe in K-Ba122 near optimal doping ($T_c \approx 37$ K).

If the gap is small on some part of the Fermi surface, compared to the maximum value that dictates $H_c$, this will
make it easier to excite quasiparticles, and so lead to an enhanced thermal conductivity at a given value of $H/H_{c2}$. This is what happens in K-Ba122 with decreasing $x$, whereby $\kappa_0/\kappa_N$ becomes larger and larger with underdoping. A good way to visualize this evolution is to plot $\kappa_0/\kappa_N$ versus $x$ at $H/H_{c2} = 0.15$, as done in Fig. 4. We infer from our in-field data that the gap structure of K-Ba122 develops a minimum somewhere on its Fermi surface, which gets deeper and deeper upon entering the coexisting antiferromagnetic phase.

This is consistent with the behavior of the in-plane penetration depth [25], which reveals a notable decrease of the superfluid stiffness in the coexistence range, and exhibits a transformation of its temperature dependence, $\Delta\lambda_\parallel(T)$, from an exponential at optimal doping to a power law with $n \approx 2$ in heavily underdoped compositions. This is a key signature of a gap structure with strong modulation, and possibly nodes, triggered by the onset of the long-range magnetic order. However, unlike our directional thermal conductivity measurements, penetration depth measurements cannot rule out the presence of accidental nodes in the gap structure.

There are two ways in which the gap can be small on part of the Fermi surface. It can develop a strong anisotropy on one sheet of the Fermi surface, as is believed to happen in borocarbide superconductors [48]. It can also be small on one surface and large on another. This multiband scenario is what happens in MgB$_2$ (Ref. [49]) and NbSe$_2$ (Ref. [44]). In both cases, $\kappa_0/\kappa_N$ grows fast, according to a field scale $H^*$ much smaller than $H_{c2}$, as it is controlled by the minimum gap. See Fig. 2 for the data on NbSe$_2$.

The third property of the $\kappa_0/\kappa_N$ versus $H$ data in Fig. 2 is its isotropy with respect to current direction. The same behavior is observed for in-plane and interplane heat currents. This implies that the minima which develop in the gap structure have no strong $k_\parallel$ dependence, i.e., they run vertically along the $c$ axis.

In Fig. 5, we provide a sketch of how the superconducting gap structure evolves with doping in K-Ba122, in terms of a simple one-band Fermi surface. Since the gap modulation has no significant $k_\parallel$ dependence, we limit our discussion to a two-dimensional picture. At high $x$, the gap is isotropic (panel c), meaning that there is no indication of any modulation of the gap with angle. Upon lowering $x$, the gap acquires a modulation, with a minimum gap $\Delta_{\text{min}}$ along some direction (panel b), and the gap minimum deepens with decreasing $x$ (panel a). This explains why the initial rise in $\kappa_0/\kappa_N$ versus $H$ gets steeper with decreasing $x$ (Fig. 2).

The question is: why does the gap develop a modulation? In a number of calculations applied to pnictides, the so-called $s_{\pm}$ state is the most stable. This is a state with $s$-wave symmetry but with a gap that changes sign in going from the holelike Fermi surface centered at $\Gamma$ ($\Delta_0 > 0$) to the electronlike Fermi surfaces centered at $X$ and $M$ ($\Delta_0 < 0$) [50–52]. Although fundamentally nodeless, the associated gap function can have strong modulations, depending on details of the Fermi surface and the interactions, possibly leading to accidental nodes [35]. The gap modulation comes from a strongly anisotropic pairing interaction, which is also band dependent, involving the interplay of intraband and interband interactions. It is typically the gap on the electron Fermi surface centered at the $M$ point of the Brillouin zone that shows a strong angular dependence.
A broad range of doping, up to order in K-Ba122 coexists with superconductivity over a same concentration, as seen in Fig. 4. The modulation of the gap and the magnetic order appear at the onset of antiferromagnetic order. This is based on the fact that underdoped side of the phase diagram, having to do with the change in interactions [20].

We propose that another mechanism is at play on the underdoped side of the phase diagram, having to do with the onset of antiferromagnetic order. This is based on the fact that the modulation of the gap and the magnetic order appear at the same concentration, as seen in Fig. 4.

Neutron-scattering studies show that antiferromagnetic order in K-Ba122 coexists with superconductivity over a broad range of doping, up to \( x \approx 0.25 \) (\( T_c \approx 26 \text{ K} \)), and both magnetism and superconductivity are bulk and occupy at least 95% of the sample volume [53]. The fact that \( k_0 / T = 0 \) for \( H = 0 \) in all our samples rules out a scenario of phase separation, whereby significant portions of the sample are not superconducting.) This bulk coexistence is deemed to be a strong argument in favor of the \( s^\pm \) model, and one against the usual \( s \)-wave scenario [54,55].

Antiferromagnetism in K-Ba122 causes a reconstruction of the Fermi surface whereby the \( \Gamma \)-centered hole pocket becomes superimposed on the edge-centered electron pocket, as sketched in Fig. 6. Energy gaps open at the points where the original two Fermi pockets cross, resulting in the formation of four small crescent-shaped pieces (Fig. 6). Maiti et al. [36] showed theoretically that such a reconstruction triggers a strong modulation of the superconducting gap, which develops strong minima, and possibly even (accidental) nodes, at the crossing points. It therefore seems natural to attribute the appearance of gap minima in underdoped K-Ba122 to the onset of magnetic order.

It is known that the orthorhombic distortion and the superconductivity are intimately coupled in KBa122 [56]. It was shown theoretically that when both the superconducting and the orthorhombic order parameters are taken into account the anisotropy of the superconducting coherence length can be greatly enhanced [57]. This could also explain the appearance of the gap anisotropy in this material.

In underdoped Co-Ba122, a similar thermal conductivity study revealed that a strong modulation of the gap also appears with the onset of magnetic order [20]. So the two materials tell a consistent story. In Fig. 7, we compare the evolution of the gap as found in thermal conductivity measurements on the two sides of the phase diagram of BaFe\(_2\)As\(_2\): the electron-doped side (Co-Ba122) and the hole-doped side (K-Ba122). In both cases, the gap is isotropic close to optimal doping, and it develops a strong modulation with underdoping, concomitant with the onset of antiferromagnetism.

However, there is a difference between K-Ba122 and Co-Ba122. The former does not develop nodes, while the latter does. These nodes are in regions of the Fermi surface with strong dispersion, as they give rise to a large zero-field value of \( k_0 / T \) for \( J || c \), but not for \( J || a \) (Fig. 7, bottom panel) [20].

**V. SUMMARY**

In summary, the thermal conductivity of K-Ba122 in the \( T = 0 \) limit reveals three main facts. First, the superconducting...
gap at optimal doping, where $T_c$ is maximal, is isotropic, with no sign of significant modulation anywhere on the Fermi surface. This reinforces the statement made earlier on the basis of thermal conductivity data in Co-Ba$_{122}$ [20], that superconductivity in pnictides is strongest when isotropic, pointing fundamentally to a state with $s$-wave symmetry, at least in the high-$T_c$ members of the pnictide family. Secondly, with underdoping, the superconducting gap becomes small in some parts of the Fermi surface. The minimum gap gets weaker and weaker with decreasing $x$. Because this modulation of the gap appears with the onset of antiferromagnetic order, we attribute it to the associated reconstruction of the Fermi surface. Third, although it acquires minima, the superconducting gap structure of underdoped K-Ba$_{122}$ never develops nodes, where the gap goes to zero. This is in contrast with underdoped Co-Ba$_{122}$, the gap of which does have nodes.

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