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Thermodynamic signatures of quantum criticality in cuprate superconductors

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SUPPLEMENTARY INFORMATION

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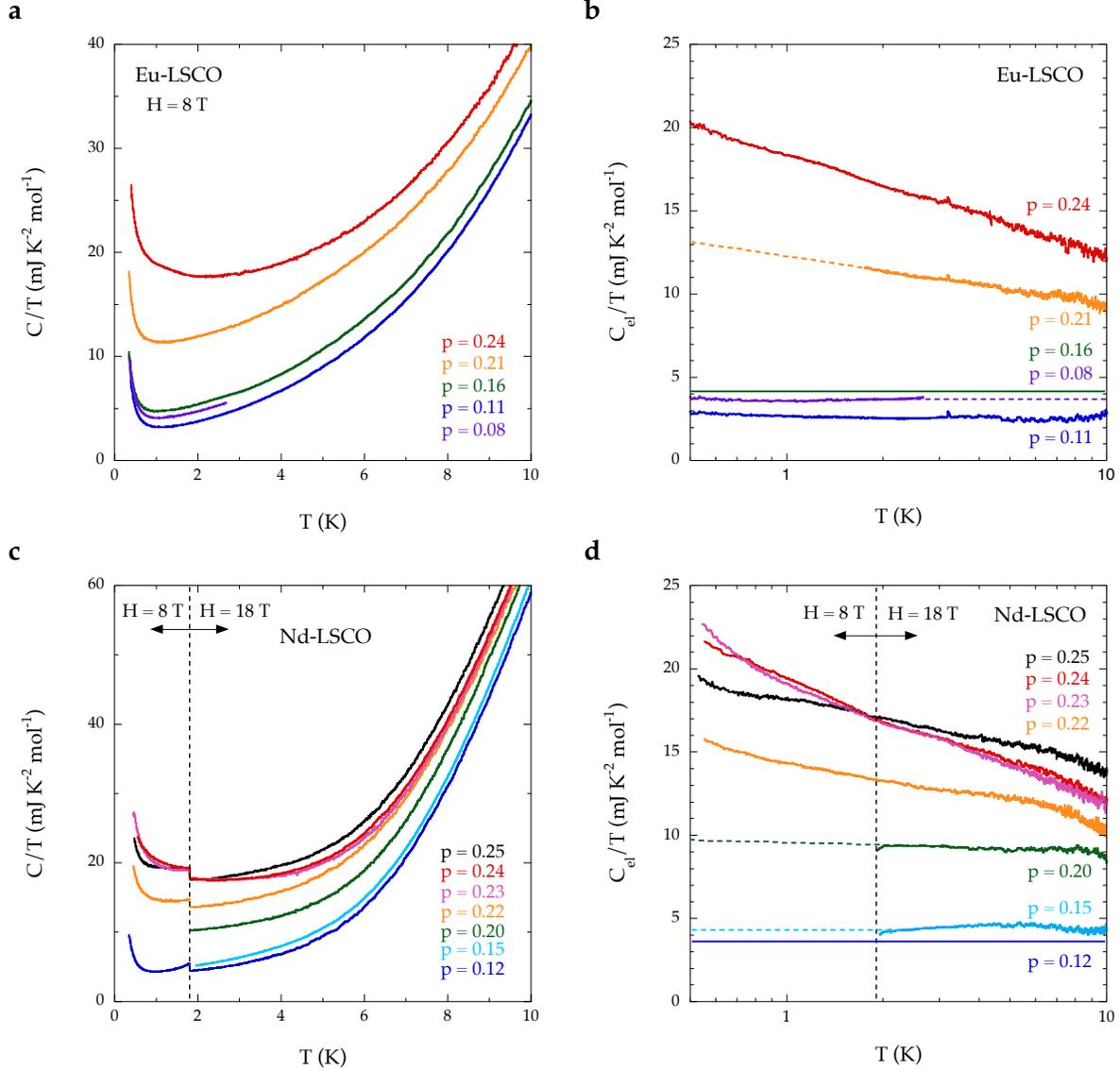
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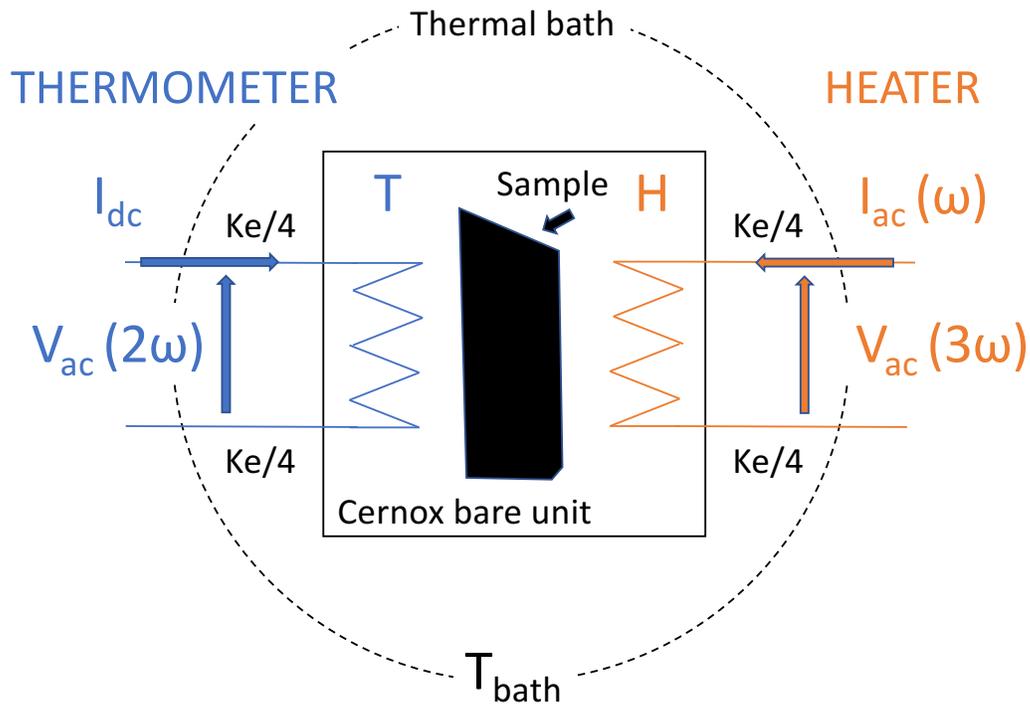
Supplementary Figure 2

Supplementary Figure 3



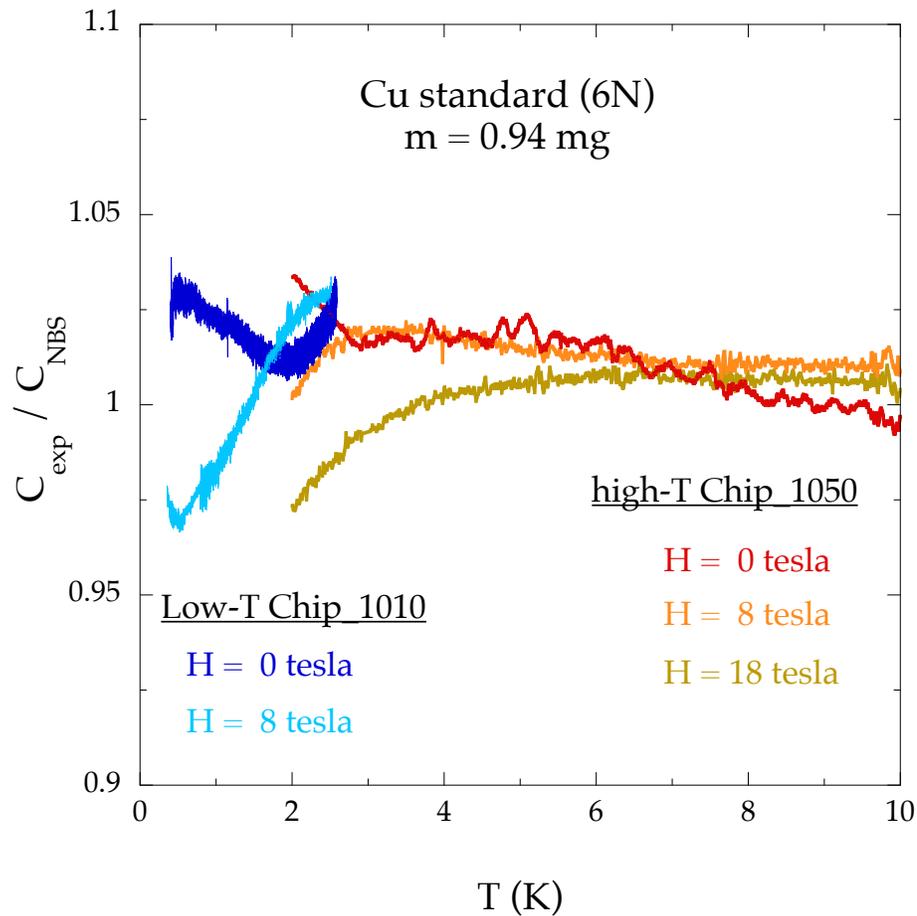
Supplementary Fig. 1 | Specific heat data for all crystals of Eu-LSCO and Nd-LSCO.

a) Specific heat of our five Eu-LSCO crystals measured in a field $H = 8$ T, down to 0.4 K. The rapid rise below 1 K is a nuclear Schottky anomaly (C_{nuclear}). **b)** Electronic specific heat $C_{el}(T)$ of those five Eu-LSCO crystals, plotted as C_{el}/T vs $\log T$, from data at $H = 8$ T ($p = 0.08, 0.11, 0.16, \text{ and } 0.24$) and at $H = 18$ T ($p = 0.21$). $C_{el}(T)$ is defined as $C_{el}(p; T) = C(p; T) - C(p=0.16; T) + \gamma$, where $\gamma = 4.2$ mJ /K² mol is the residual linear term of the $p = 0.16$ reference data ($C/T = \gamma + \beta T^2$, in Fig. 2a). Dashed lines are a linear extrapolation of the data ($p = 0.21$, orange; $p = 0.08$, purple). **c)** Same as panel **a**, for our seven Nd-LSCO crystals ($H = 8$ T, below the dashed line; $H = 18$ T, above the dashed line). **d)** Same as panel **b**, for those seven crystals, using data at $p = 0.12$ as the reference curve for subtraction, with $\gamma = 3.6$ mJ /K² mol (Fig. 2c).



Supplementary Fig. 2 | Experimental setup for the measurement of heat capacity.

Sketch of our experimental setup, showing the bare Cernox chip (black square) suspended by four PtW wires. A shallow groove is made with a wire saw to obtain two independent sides, one for the heater (H, right side) and one for the thermometer (T, left side). The sample is glued with a minute amount of Apiezon grease on the back of the sapphire substrate. An AC current I_{ac} at a frequency ω is applied across the heater to induce temperature oscillations of the small platform (sample + Cernox). A DC current I_{dc} is applied across the thermometer whose voltage is demodulated at 2ω (see METHODS – Specific heat measurements).



Supplementary Fig. 3 | Test of our specific heat measurement on a Cu sample.

Specific heat C_{exp} of a sample of copper measured using the same setup and analysis as used for our samples of Eu-LSCO and Nd-LSCO, plotted as $C_{\text{exp}} / C_{\text{NBS}}$ vs T , where C_{NBS} is the standard value of the specific heat of copper established by the National Bureau of Standards. The measured data never deviate by more than 2-3 % from the standard, over the full temperature range from 0.5 K to 10 K, whether taken in the ^4He refrigerator at $H = 0, 8$ and 18 T (using a Cernox 1050 thermometer) or the ^3He refrigerator at $H = 0$ and 8 T (using a Cernox 1010 thermometer).