Anisotropic Seebeck coefficient of Sr₂RuO₄ in the incoherent regime

Ramzy Daou, ¹ Sylvie Hébert ¹, ¹ Gaël Grissonnanche ¹, ² Elena Hassinger, ² Louis Taillefer ¹, ² Haruka Taniguchi, ³, ⁴ Yoshiteru Maeno ¹, ³, ⁵ Alexandra S. Gibbs, ⁶ and Andrew P. Mackenzie ⁶

¹ Normandie Univ, ENSICAEN, UNICAEN, CNRS, CRISMAT, 14000 Caen, France

² Département de physique & RQMP, Université de Sherbrooke, Sherbrooke, Québec JIK 2R1, Canada

³ Department of Physics, Kyoto University, Kyoto 606-8502, Japan

⁴ Department of Applied Physics, Graduate School of Engineering, Nagoya University, Nagoya, 464-8603, Japan

⁵ Toyota Riken - Kyoto Univ. Research Center (TRiKUC), Kyoto 606-8501, Japan

⁶ Max Planck Institute for Chemical Physics of Solids, Nöthnitzer Str. 40, 01187 Dresden, Germany



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Intuitive entropic interpretations of the thermoelectric effect in metals predict an isotropic Seebeck coefficient at high temperatures in the incoherent regime even in anisotropic metals since entropy is not directional. Sr₂RuO₄ is an enigmatic material known for a wellcharacterized anisotropic normal state and unconventional superconductivity. Recent *ab initio* transport calculations of Sr₂RuO₄ that include the effect of strong electronic correlations predicted an enhanced high-temperature anisotropy of the Seebeck coefficient at temperatures above 300 K, but experimental evidence is missing. From measurements on clean Sr₂RuO₄ single crystals along both crystallographic directions, we find that the Seebeck coefficient becomes increasingly isotropic upon heating towards room temperature as generally expected. Above 300 K, however, *S* acquires a new anisotropy which rises up to the highest temperatures measured (750 K), in qualitative agreement with calculations. This is a challenge to entropic interpretations and highlights the lack of an intuitive framework to understand the anisotropy of thermopower at high temperatures.

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Introduction. The layered perovskite Sr₂RuO₄ has been studied intensively since it was found to host an unconventional superconducting ground state [1]. A wide range of thermodynamic, transport, and spectroscopic experiments have examined both the superconducting [2] and normal states [3], especially at low temperatures. Ab initio electronic structure calculations provide increasingly good agreement with experimental observations, but consensus is lacking on the precise nature of the superconducting order parameter as well as the pairing mechanism.

The normal-state electronic structure is characterized by three bands arising mainly from Ru 4d states. A renormalized ground state with enhanced effective mass indicates the presence of strong correlations. Above the modest Fermi liquid temperature of $\sim\!25$ K, there is a crossover from the regime of coherent, well-realized quasiparticles into the "incoherent" regime where the excitation spectrum lacks a well-defined Drude peak. A feature of note is the peak in c-axis resistivity that occurs around 150 K that has yet to be satisfactorily explained [4].

It has only become possible for *ab initio* calculations to reproduce experimentally observed trends in transport properties in strongly correlated materials in the last few years. Recently, dynamical mean-field theory (DMFT) calculations have predicted an enhancement of the out-of-plane Seebeck coefficient of Sr_2RuO_4 at high temperatures [5].

The Seebeck coefficient S quantifies the relationship between charge and heat transport in a conductor. While it is a transport property, it does not depend on the dimensions of the sample. Its existence can be derived in the absence

of scattering purely from thermodynamic considerations [6]. It has therefore been argued that in limit of either low [7] or high temperature [8,9], it scales linearly with the entropy associated with the charge carriers. A further implication is that in these limits *S* should be isotropic, since the entropy is not a directional quantity. This interpretation makes it useful in separating, for example, the entropy associated with charge carriers from other sources such as lattice vibrations.

In this Letter, we show measurements of the Seebeck coefficient of $\rm Sr_2RuO_4$ in both in- and out-of-plane directions on high quality single crystals up to 750 K that confirm the trends predicted by numerical calculations. Upon heating up towards room temperature, the Seebeck coefficient becomes increasingly isotropic, as generally expected. Above around 300 K, which corresponds to the regime of incoherent transport, S acquires a new anisotropy, which rises up to the highest temperatures measured (750 K). This high-temperature anisotropy is the subject of this paper.

The Seebeck coefficient was measured using a standard one-heater, two-thermometer steady-state technique from 2–320 K as described in Ref. [10]. Fine-wire thermocouples were attached directly to the samples to measure the temperature difference. The thermoelectric voltage was measured against phosphor-bronze reference leads. The contribution to the Seebeck signal was negligible (<0.1 μVK^{-1}) in this range and has not been subtracted from the data.

In the temperature range 300-800 K, S was measured using a two-heater, two-thermometer technique on a miniature high-temperature sample holder designed to fit into a standard physical properties measurement system cryostat. The

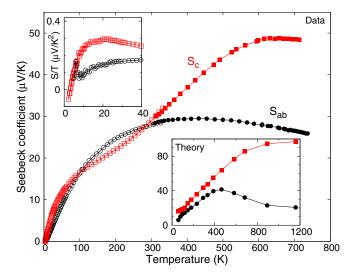


FIG. 1. Seebeck coefficient of Sr_2RuO_4 up to 800 K for samples 1 (S_{ab} , circles) and 2 (S_c , squares). The low-temperature (open symbols) and high-temperature (closed symbols) data overlap well. S_c continues to increase above 300 K while S_{ab} reaches a maximum around 400 K and decreases slightly thereafter. Upper inset: low-temperature data plotted as S/T. Lower inset: DMFT calculations of S_{ab} and S_c from Ref. [5].

reduced size of the experiment allows us to reach high temperatures without applying more heat than the cryostat can safely dissipate. Two two-wire type-E thermocouples made of 25 µm diameter wire were used to measure the temperature at two points along the sample. Two platinum-wire heaters were used to apply the temperature gradient, which could be reversed. The thermoelectric voltage was measured with reference to the chromel leads of the thermocouples. The temperature and voltage were therefore sensed at exactly the same points, directly at the sample. The Seebeck coefficient was extracted from the linear slope of the voltage as a function of the applied temperature difference between the thermocouples; no nonlinearity was observed. To obtain the Seebeck coefficient of the chromel reference leads, we measured a high-purity platinum wire as a reference up to 800 K and subtracted its contribution [11] which is known with an accuracy of around $\pm 0.2 \,\mu\text{VK}^{-1}$. The precision of the measurement is indicated by the scatter of the points ($< 1 \mu V K^{-1}$ everywhere). If there are additional systematic errors associated with, e.g., thermal radiation losses at high temperatures, the use of very similarly sized samples ensures that the results are comparable.

The $\rm Sr_2RuO_4$ single crystals used in this study were grown by a floating zone technique. For *ab*-plane measurements we used a crystal of size $3.0 \times 0.8 \times 0.3 \ \rm mm^3$. For *c*-axis measurements the sample measured $0.3 \times 0.4 \times 3.0 \ \rm mm^3$.

The results over an extended temperature range up to 800 K are shown in Fig. 1. The overlap between high- and low-temperature data from different experimental setups is good, which validates the experimental protocols particularly with respect to the use of different reference leads (phosphorbronze at low temperature, chromel at high temperature).

Up to 300 K S_{ab} matches existing results [12,13] well. There is a smooth rise from zero with a gradual decrease of slope. S_c meanwhile is of similar magnitude to S_{ab} below

200 K, although there are changes in slope where S_{ab} appears smooth, and the approach to low temperatures of S_c is steeper. At very low temperatures (see inset to Fig. 1) S_c appears to change sign, although this should be confirmed by a more sensitive low-temperature technique.

Above 300 K, S_{ab} reaches a maximum of 28 μ VK⁻¹ at around 400 K and then declines gradually up to the highest measured temperature of 780 K. A plateau in the value of S at around 30 μ VK⁻¹ is a common feature of many ruthenium oxides [14]. The data in this temperature range is compatible with a measurement on sintered polycrystalline material [15].

It is only above 300 K where S_c becomes considerably greater in absolute terms than S_{ab} , reaching nearly 50 μ VK⁻¹ at 600 K before leveling off at higher temperatures. The structure of $S_c(T)$ is clearly of interest. The out-of-plane resistivity ρ_c peaks at \sim 150 K. This has been interpreted as a sign of the crossover between coherent transport at lower temperatures and incoherent transport at higher temperatures [16]. A point of inflection in the temperature dependence of S_c occurs at a similar temperature.

This feature is unlikely to be related to phonon drag, as this generally requires that phonon transport in the same direction be out-of-equilibrium. This condition is usually only seen in the clean limit where the momentum-conserving electron-phonon scattering rate can outweigh the momentum-relaxing processes such as defect, impurity, and umklapp scattering. While this might be achieved at low temperatures in Sr₂RuO₄, it is unlikely to be the case at 150 K. The lack of a definitive phonon drag signature even in the low-resistance in-plane direction (typically a strong enhancement of *S* at some fraction of the Debye temperature, with a dependence on sample purity) argues against phonon drag as an active mechanism.

Entropic interpretations. In the low-temperature limit, the slope of the Seebeck coefficient has been shown to track the electronic part of the specific heat with a proportionality fixed only by fundamental constants [7]. From the measured value of the electronic specific heat in the normal state [17], we would expect $|S|/T \approx 0.4 \, \mu V K^{-2}$ as $T \to 0$. Comparison to the inset of Fig. 1 shows that the data is of the correct order of magnitude, but that the low-temperature limit has not been reached. Generally, in multiband strongly correlated materials, the expected relationship is only seen at temperatures below 1 K [7].

At high temperature, the Heikes formula is derived in the atomic limit where transport proceeds by hopping between isolated sites [8]. The Seebeck coefficient is given by $S_H = -(1/e)(\frac{\partial S_e}{\partial n}|_E)$ where S_e is the entropy and n is the carrier density. An alternative to this is the very similar Kelvin formula $S_K = -(1/e)(\frac{\partial S_e}{\partial n}|_T)$, which is derived by taking transport formulas to the thermodynamic limit [9]. In each case the Seebeck coefficient claims to be a measure of the entropy associated with each particle.

Numerical evaluation of S_H and S_K for Sr_2RuO_4 [5] produce values that are not too far away from the experimental ones at high temperature, at least for S_{ab} . The continued rise of S_C with T is not, however, captured by these calculations.

The other relevant implication of this interpretation is that *S* should become isotropic in the limit of both high and low temperature if it is purely a reflection of the entropy transported by a carrier. However, as is seen here

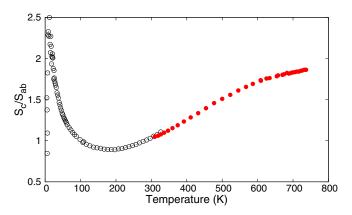


FIG. 2. Anisotropy of the Seebeck coefficient S_c/S_{ab} as a function of temperature. From around 100–300K it is close to unity and becomes larger below and above.

and in other materials such as BEDT-TTF [18] and Nd-LSCO [19], anisotropy persists over a large temperature range.

Semiclassical transport. The transport coefficients in metallic materials generally depend on the scattering and dispersion of quasiparticles in an energy window of order $\pm 5k_BT$ around ε_F . Here, S_c only becomes very different from S_{ab} for T>300 K. If the assumptions of semiclassical transport hold at these high temperatures, this is an indication that it is states further than ± 0.1 eV from ε_F which contribute to changes in the anisotropy. S_{ab} calculated from the electronic band structure [5] has a quasilinear temperature dependence that does not at all resemble the data. There is a significant peak in the out-of-plane transport function, but it is 1 eV below ε_F and could therefore not be the origin of any feature in S_c observed here.

Some recent work has focused on the impact of the van Hove singularity in the γ band on transport [20–22]. At only 14 meV above the Fermi level, the associated peak in the density of states should impact the Seebeck coefficient at lower temperatures than the apparent onset of anisotropy. It might therefore be tempting to assign the intermediate-temperature features in S_c to the presence of this van Hove singularity. However, the lack of associated features in S_{ab} is difficult to understand without invoking an additional directional mechanism.

Mott formula. The Seebeck coefficient is expected to be relatively isotropic if it is governed by a single energy scale, even if the electrical conductivity is anisotropic. This can be understood by reference to the Mott formula, which relates the Seebeck coefficient to the electrical conductivity

$$S_i = \frac{\pi^2}{3} \frac{k_B}{e} T \frac{\partial (\ln \sigma_i)}{\partial \varepsilon} \bigg|_{\varepsilon = \varepsilon_F}. \tag{1}$$

The logarithmic derivative means that the Seebeck coefficient is much less sensitive to anisotropy in the electronic band structure than the conductivity. Even modest anisotropy in S could therefore be an indication of a significant difference in the energy scale governing scattering in the two directions. The anisotropy S_c/S_{ab} is shown in Fig. 2. While the low-temperature behavior (up to 100 K) can be reasonably

assigned to anisotropy originating in the electronic structure, it is by no means clear that the picture of semiclassical transport is still valid as the temperature increases further and the mean free path drops to the order of the lattice spacing. It is difficult therefore to explain the anisotropy in *S* at high temperature using the Mott relation.

In one quasi-2D layered material PdCoO₂, a thermoelectric anisotropy of \sim 50 has been predicted to arise purely from band effects [23], but this has not been experimentally verified. The crucial factor behind this is the strong variation of the warping in the k_z direction of the quasicylindrical Fermi surfaces as a function of energy. More typical is the case of intercalated graphite, where the thermoelectric power is anisotropic, but only by a factor of two, while the conductivity anisotropy is around 1000 [24,25].

In Sr₂RuO₄, La-substitution was shown to donate electrons and induce a rigid shift of the electronic bands with respect to the Fermi energy, while introducing minimal disorder [26]. The anisotropy in conductivity changes little [27], however, and we therefore expect *S* to be isotropic at low temperatures, assuming that the changes in conductivity arise purely from the rigid shifting of the bands.

DMFT calculations. DMFT was used to calculate the transport coefficients of Sr_2RuO_4 in Ref. [5]. A peak in the kernel of the out-of-plane transport integral was found at an energy ~ 0.3 eV below the Fermi energy, causing an enhancement of S_c at temperatures approaching $\gtrsim 300$ K.

While S_c is found to be greater than S_{ab} everywhere, it is above 400 K that the calculated values begin to diverge considerably. The results of this calculation are reproduced in Fig. 1. The significant trend in the experimental data is followed well.

Transport calculations using the semiclassical model failed to reproduce either the rapid initial rise of S_{ab} or the subsequent plateau. The semiquantitative agreement of the data with DMFT shows that electron-electron correlations must be taken into account. The implication is that S cannot generally be treated as a thermodynamic quantity, although S_H and S_K can be useful guides to the expected order of magnitude in the high temperature limit.

A similar conclusion was drawn from a recent exploration of the temperature dependence of the Hall effect [20], which argued against the fine tuning that multiband semiclassical transport calculations require to reproduce experimental data.

Comparison to other materials. The organic superconductor κ -(BEDT-TTF) $_2Cu[N(CN)_2]Br$ displays a marked ansiotropy of S within the conducting plane, as a result of quasi-1D features of the electronic structure [18]. While a tight-binding model was able to reproduce the signs and temperature dependence of S up to 300 K quite well, the bandwidth had to be artificially reduced to obtain this agreement, suggesting that strong correlations had to be taken into account. Like Sr_2RuO_4 , $\kappa - (BEDT - TTF)_2Cu[N(CN)_2]Br$ has a relatively low coherence temperature of around 50 K. DMFT calculations [28] later treated the crossover into the incoherent regime and were able to reproduce the features seen in S.

The high temperature cuprate superconductors are also incoherent, anisotropic metals in their normal state. In La_{2-x}Sr_xCuO₄ the temperature evolution of the Seebeck

coefficient measured within and perpendicular to the CuO_2 planes is very reminiscent of Sr_2RuO_4 [29]. At x = 0.10, the magnitudes and anisotropy are similar to that seen in Sr_2RuO_4 , with S_{ab} rising to a broad maximum, while S_c continues to rise up to 300 K. On further doping, S_{ab} drops and changes sign while S_c retains similar features.

A recent study on Nd-La_{2-x}Sr_xCuO₄ [19], where superconductivity and its associated impact on transport is suppressed to low temperatures, also revealed strong anisotropy across a wide range of doping. A particular feature is the appearance of nonmonotonic features in $S_c(T)$ at around 100 K, which are not seen in S_{ab} . This parallel with Sr₂RuO₄ merits further investigation.

Conclusions. We observe a strong anisotropy in the Seebeck coefficient of Sr_2RuO_4 at temperatures above 300 K, in accordance with predictions of transport calculations. The

out-of-plane Seebeck coefficient contains features at an intermediate temperature similar to that of the peak in *c*-axis resistivity which merit further consideration. The isotropic behavior predicted by arguments based on the entropy of the carriers is not realized, neither at the moderately high temperatures where these interpretations have enjoyed some success [30,31], nor at temperatures down to 5 K. While *ab initio* calculations do appear to provide some insight, these results highlight the lack of an intuitive framework to understand the anisotropy of thermopower at high temperatures.

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- [1] A. P. Mackenzie, T. Scaffidi, C. W. Hicks, and Y. Maeno, Even odder after twenty-three years: The superconducting order parameter puzzle of Sr₂RuO₄, npj Quantum Mater. **2**, 40 (2017).
- [2] A. P. Mackenzie and Y. Maeno, The superconductivity of Sr₂RuO₄ and the physics of spin-triplet pairing, Rev. Mod. Phys. 75, 657 (2003).
- [3] C. Bergemann, A. P. Mackenzie, S. R. Julian, D. Forsythe, and E. Ohmichi, Quasi-two-dimensional Fermi liquid properties of the unconventional superconductor Sr₂RuO₄, Adv. Phys. 52, 639 (2003).
- [4] A. W. Tyler, A. P. Mackenzie, S. NishiZaki, and Y. Maeno, High-temperature resistivity of Sr₂Ruo₄: Bad metallic transport in a good metal, Phys. Rev. B **58**, R10107(R) (1998).
- [5] J. Mravlje and A. Georges, Thermopower and Entropy: Lessons from sr₂ruo₄, Phys. Rev. Lett. **117**, 036401 (2016).
- [6] H. B. Callen, The application of onsager's reciprocal relations to thermoelectric, thermomagnetic, and galvanomagnetic effects, Phys. Rev. **73**, 1349 (1948).
- [7] K. Behnia, D. Jaccard, and J. Flouquet, On the thermoelectricity of correlated electrons in the zero-temperature limit, J. Phys.: Condens. Matter 16, 5187 (2004).
- [8] P. M. Chaikin and G. Beni, Thermopower in the correlated hopping regime, Phys. Rev. B 13, 647 (1976).
- [9] M. R. Peterson and B. S. Shastry, Kelvin formula for thermopower, Phys. Rev. B 82, 195105 (2010).
- [10] R. Daou, R. Frésard, S. Hébert, and A. Maignan, Large anisotropic thermal conductivity of the intrinsically two-dimensional metallic oxide PdCoO₂, Phys. Rev. B **91**, 041113 (2015).
- [11] A. Burkov, A. Heinrich, P. Konstantinov, T. Nakama, and K. Yagasaki, Experimental set-up for thermopower and resistivity measurements at 100–1300 k, Meas. Sci. Technol. **12**, 264 (2001).
- [12] H. Yoshino, K. Murata, N. Shirakawa, Y. Nishihara, Y. Maeno, and T. Fujita, Thermopower of a layered perovskite superconductor, Sr₂RuO₄, J. Phys. Soc. Jpn. **65**, 1548 (1996).
- [13] X. F. Xu, Z. A. Xu, T. J. Liu, D. Fobes, Z. Q. Mao, J. L. Luo, and Y. Liu, Band-Dependent Normal-State Coherence in Sr₂RuO₄:

- Evidence from Nernst Effect and Thermopower Measurements, Phys. Rev. Lett. **101**, 057002 (2008).
- [14] S. Hébert, R. Daou, and A. Maignan, Thermopower in the quadruple perovskite ruthenates, Phys. Rev. B 91, 045106 (2015).
- [15] N. Keawprak, R. Tu, and T. Goto, Thermoelectric properties of Sr-Ru-O compounds prepared by spark plasma sintering, Mater. Trans. 49, 600 (2008).
- [16] N. E. Hussey, A. P. Mackenzie, J. R. Cooper, Y. Maeno, S. Nishizaki, and T. Fujita, Normal-state magnetoresistance of Sr₂RuO₄, Phys. Rev. B 57, 5505 (1998).
- [17] S. NishiZaki, Y. Maeno, and Z. Mao, Changes in the Superconducting State of Sr₂RuO₄ under Magnetic Fields Probed by Specific Heat, J. Phys. Soc. Jpn. 69, 572 (2000).
- [18] R. C. Yu, J. M. Williams, H. H. Wang, J. E. Thompson, A. M. Kini, K. D. Carlson, J. Ren, M.-H. Whangbo, and P. M. Chaikin, Anisotropic thermopower of the organic superconductor κ (BEDT TTF)₂Cu[N(CN)₂]Br, Phys. Rev. B 44, 6932 (1991).
- [19] A. Gourgout, G. Grissonnanche, F. Laliberté, A. Ataei, L. Chen, S. Verret, J.-S. Zhou, J. Mravlje, A. Georges, N. Doiron-Leyraud, and L. Taillefer, Seebeck Coefficient in a Cuprate Superconductor: Particle-Hole Asymmetry in the Strange Metal Phase and Fermi Surface Transformation in the Pseudogap Phase, Phys. Rev. X 12, 011037 (2022).
- [20] M. Zingl, J. Mravlje, M. Aichhorn, O. Parcollet, and A. Georges, Hall coefficient signals orbital differentiation in the Hund's metal Sr₂RuO₄, npj Quantum Mater. **4**, 35 (2019).
- [21] F. Herman, J. Buhmann, M. H. Fischer, and M. Sigrist, Deviation from Fermi-liquid transport behavior in the vicinity of a Van Hove singularity, Phys. Rev. B 99, 184107 (2019).
- [22] P.-Y. Yang, H. M. L. Noad, M. E. Barber, N. Kikugawa, D. Sokolov, A. P. Mackenzie, and C. W. Hicks, Probing momentum-dependent scattering in uniaxially stressed Sr₂RuO₄ through the Hall effect, arXiv:2302.07763 [cond-mat].
- [23] K. P. Ong, D. J. Singh, and P. Wu, Unusual Transport and Strongly Anisotropic Thermopower in PtCoO₂ and PdCoO₂, Phys. Rev. Lett. **104**, 176601 (2010).

- [24] M. Elzinga, D. T. Morelli, and C. Uher, Thermal transport-properties of SbCl₅ graphite, Phys. Rev. B **26**, 3312 (1982).
- [25] C. Uher and D. Morelli, Thermal transport-properties of SbCl₅-graphite and of HOPG in the c-direction, Synth. Met. **12**, 91 (1985).
- [26] N. Kikugawa, A. P. Mackenzie, C. Bergemann, R. A. Borzi, S. A. Grigera, and Y. Maeno, Rigid-band shift of the fermi level in the strongly correlated metal: Sr_{2-y}La_yRuO₄, Phys. Rev. B 70, 060508(R) (2004).
- [27] N. Kikugawa, C. Bergemann, A. P. Mackenzie, and Y. Maeno, Band-selective modification of the magnetic fluctuations in Sr₂RuO₄: A study of substitution effects, Phys. Rev. B 70, 134520 (2004).
- [28] J. Merino and R. H. McKenzie, Transport properties of strongly correlated metals: A dynamical mean-field approach, Phys. Rev. B 61, 7996 (2000).
- [29] Y. Nakamura and S. Uchida, Anisotropic transport properties of single-crystal La_{2-x}Sr_xCuO₄: Evidence for the dimensional crossover, Phys. Rev. B **47**, 8369 (1993).
- [30] D. B. Marsh and P. E. Parris, Theory of the seebeck coefficient in LaCrO₃ and related perovskite systems, Phys. Rev. B 54, 7720 (1996).
- [31] K. Berggold, M. Kriener, C. Zobel, A. Reichl, M. Reuther, R. Müller, A. Freimuth, and T. Lorenz, Thermal conductivity, thermopower, and figure of merit of La_{1-x}Sr_xCoO₃, Phys. Rev. B **72**, 155116 (2005).