

# Pseudogap $T^*$ along the Widom line of a first-order transition in doped Mott insulators

A.-M. Tremblay

G. Sordi, K. Haule, P. Sémond



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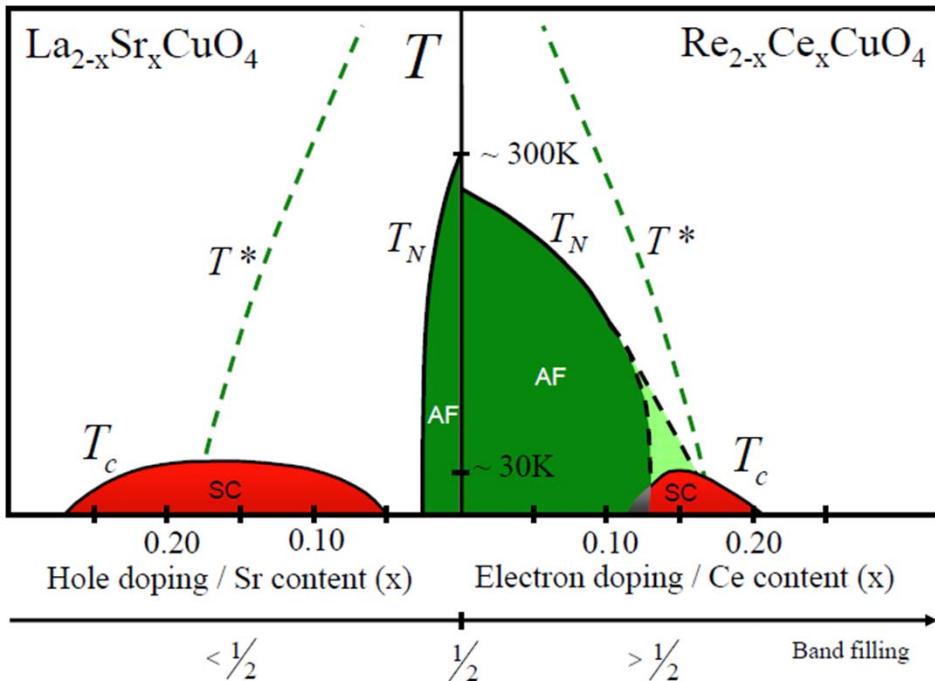
**ICSM 2012, 30 avril 2012**



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# High-temperature superconductors

Armitage, Fournier, Greene, RMP (2009)

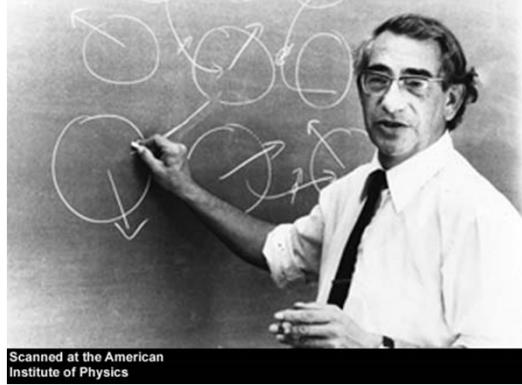


- Competing order
  - Current loops: Varma, PRB **81**, 064515 (2010)
  - Stripes or nematic: Kivelson et al. RMP **75** 1201(2003); J.C.Davis
  - d-density wave : Chakravarty, Nayak, Phys. Rev. B **63**, 094503 (2001); Affleck et al. flux phase
  - SDW: Sachdev PRB **80**, 155129 (2009) ...

- Or Mott Physics?
  - RVB: P.A. Lee Rep. Prog. Phys. **71**, 012501 (2008)

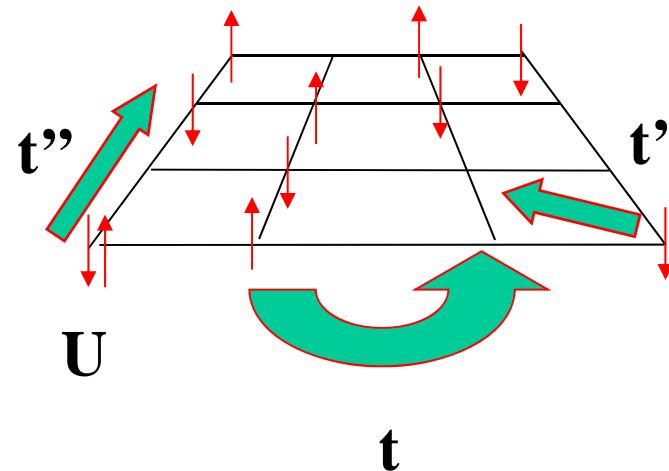
What is under the dome?  
Mott Physics away from  $n = 1$

# Hubbard model

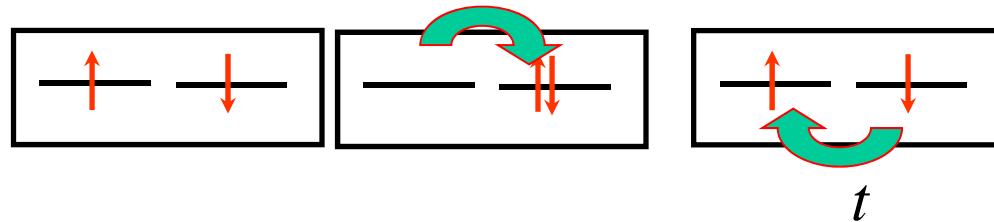


Scanned at the American  
Institute of Physics

1931-1980



$$H = -\sum_{\langle ij \rangle \sigma} t_{i,j} (c_{i\sigma}^\dagger c_{j\sigma} + c_{j\sigma}^\dagger c_{i\sigma}) + U \sum_i n_{i\uparrow} n_{i\downarrow}$$



$$t = 1$$

Effective model, Heisenberg:  $J = 4t^2 / U$



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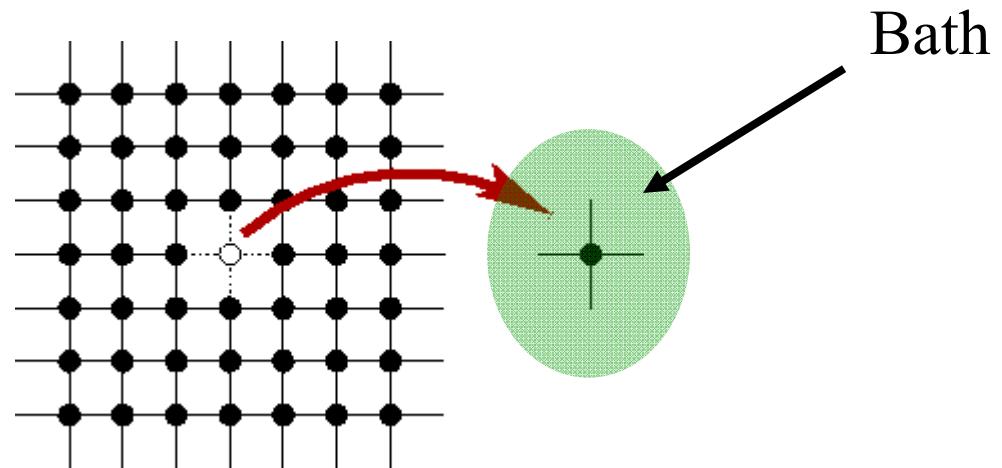
# Method



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# Mott transition and Dynamical Mean-Field Theory. The beginnings in $d = \text{infinity}$

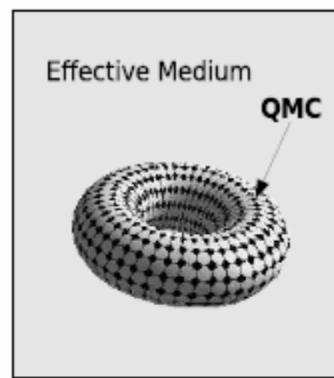
- Compute scattering rate (self-energy) of impurity problem.
- Use that self-energy ( $\omega$  dependent) for lattice.
- Project lattice on single-site and adjust bath so that single-site DOS obtained both ways be equal.



W. Metzner and D. Vollhardt, PRL (1989)  
A. Georges and G. Kotliar, PRB (1992)  
M. Jarrell PRB (1992)

DMFT, ( $d = 3$ )

# *2d Hubbard: Quantum cluster method*

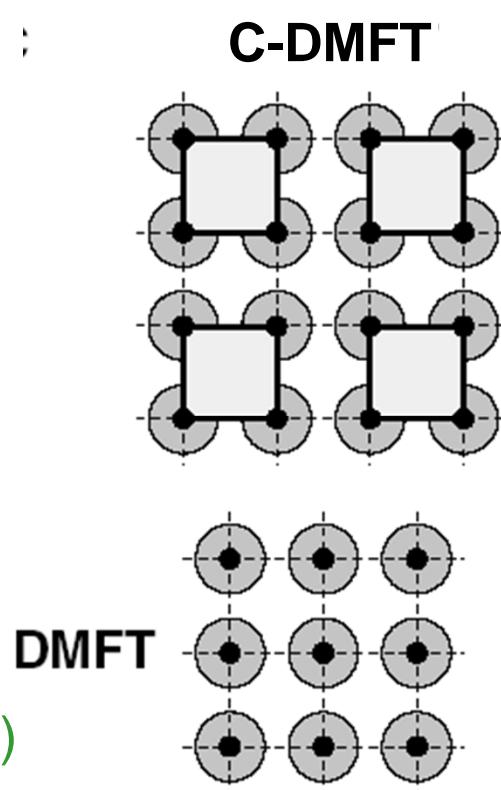


**DCA**

Hettler ... Jarrell ... Krishnamurty PRB **58** (1998)

Kotliar et al. PRL **87** (2001)

M. Potthoff et al. PRL **91**, 206402 (2003).



**REVIEWS**

Maier, Jarrell et al., RMP. (2005)

Kotliar et al. RMP (2006)

AMST et al. LTP (2006)



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# Not perfect!

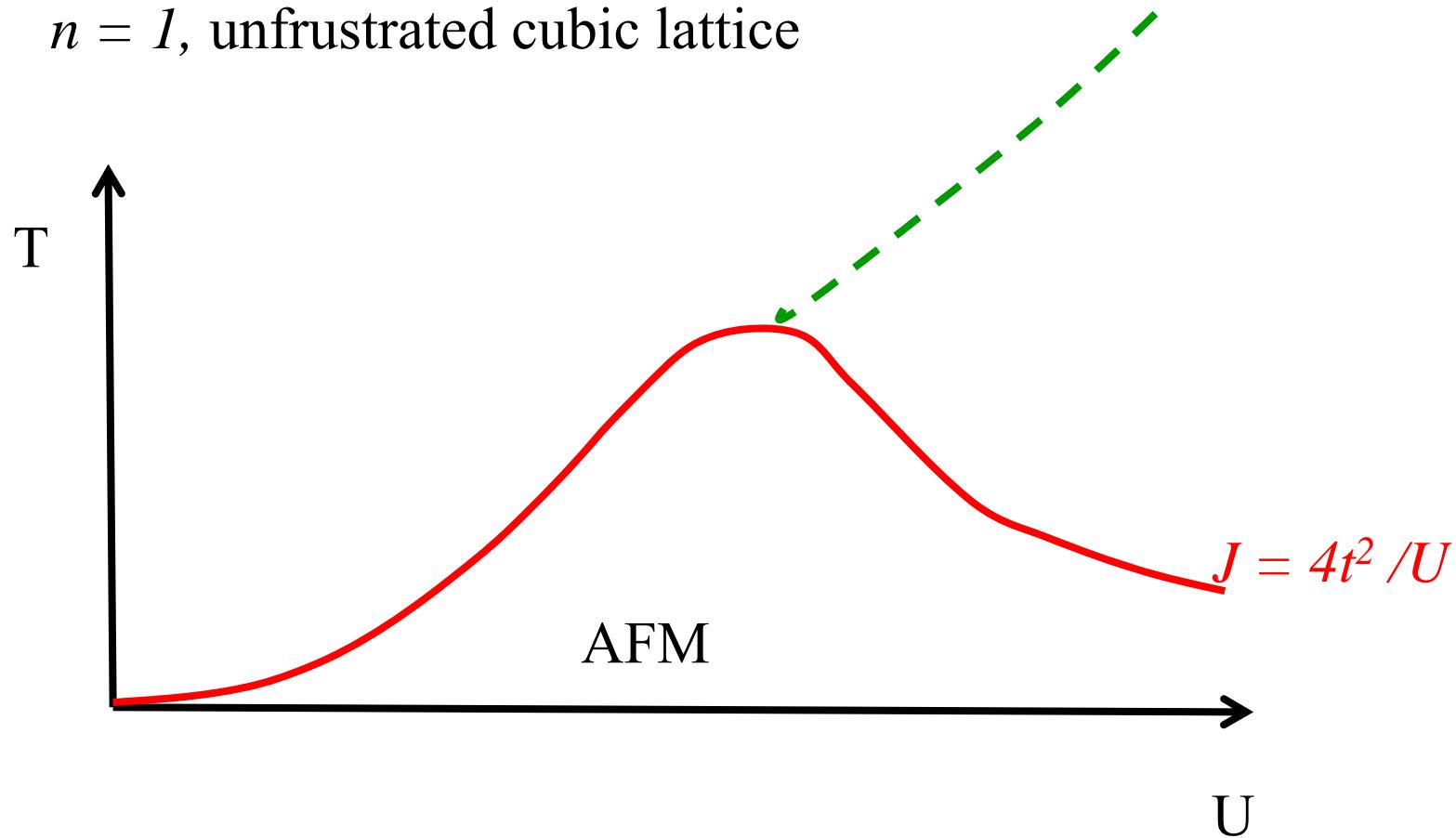
- Missing:
  - Long wavelength fluctuations
- Included:
  - Short-range dynamical and spatial correlations
- Long range order:
  - Allow symmetry breaking in the bath (mean-field)



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# Local moment and Mott transition

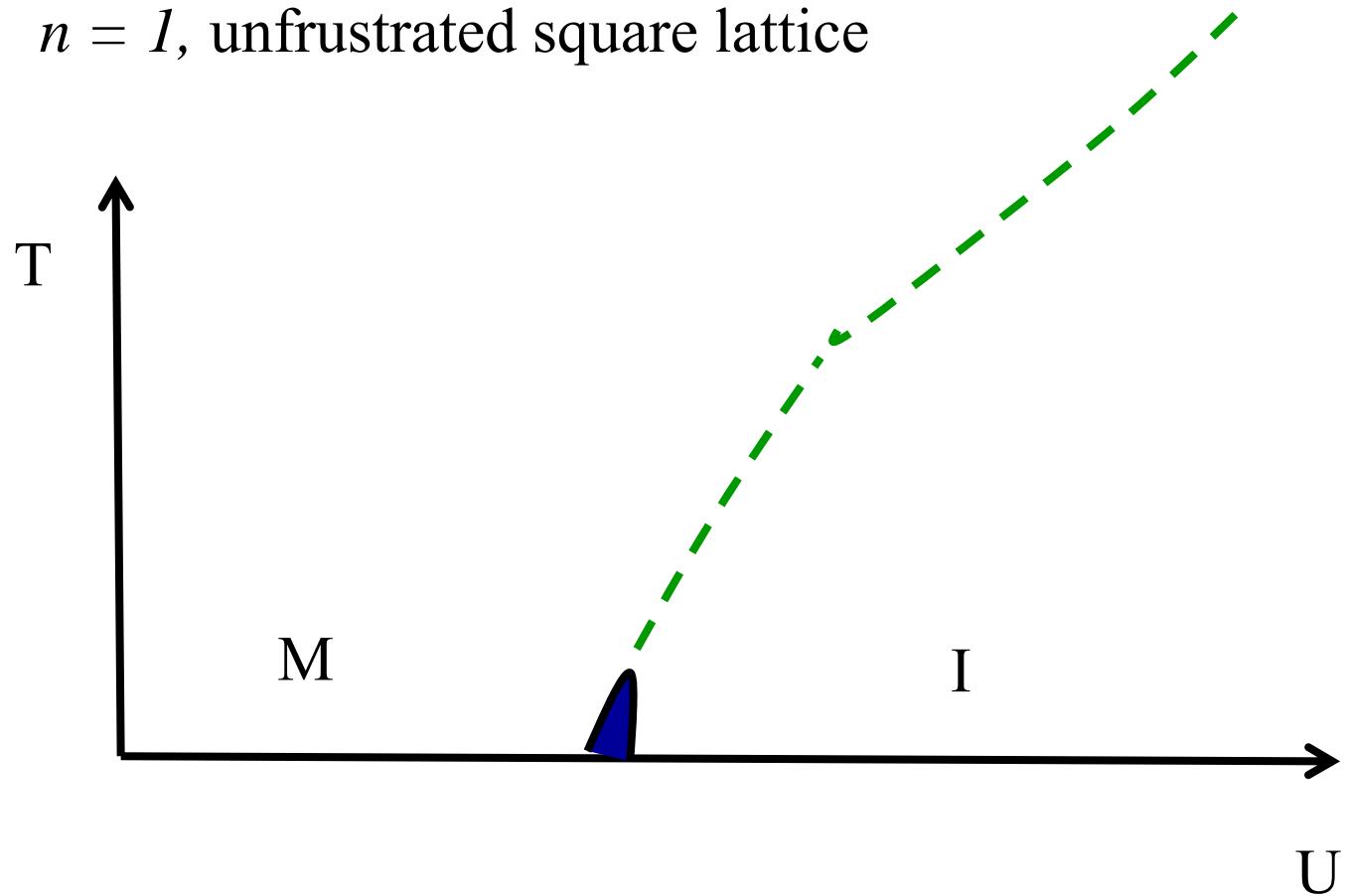
$n = 1$ , unfrustrated cubic lattice



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# Local moment and Mott transition

$n = 1$ , unfrustrated square lattice



# Outline

- Method
- Finite  $T$  phase diagram
  - Normal state (no LRO, what is below the dome)
    - First order transition
    - Widom line and pseudogap



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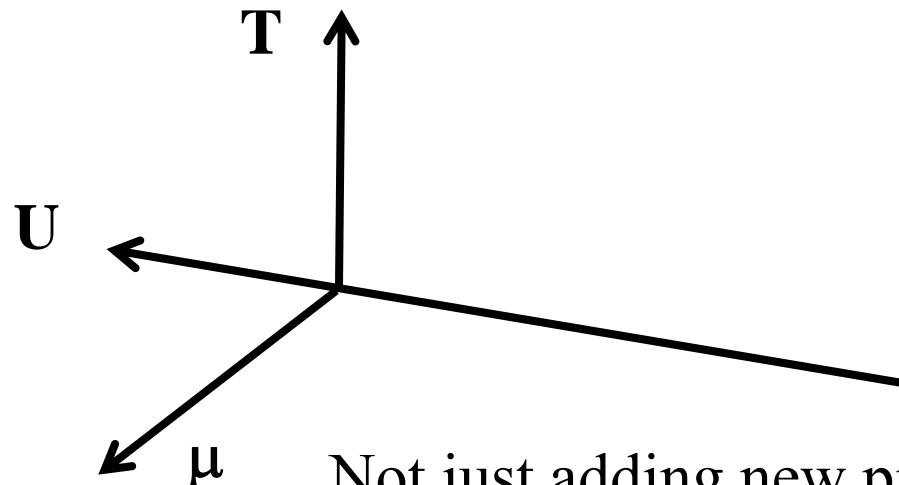


Giovanni Sordi

G. Sordi, K. Haule, A.-M.S.T  
PRL, **104**, 226402 (2010)  
and

Phys. Rev. B, **84**, 075161 (2011)

## Doping-induced Mott transition ( $t'=0$ )



Not just adding new piece:

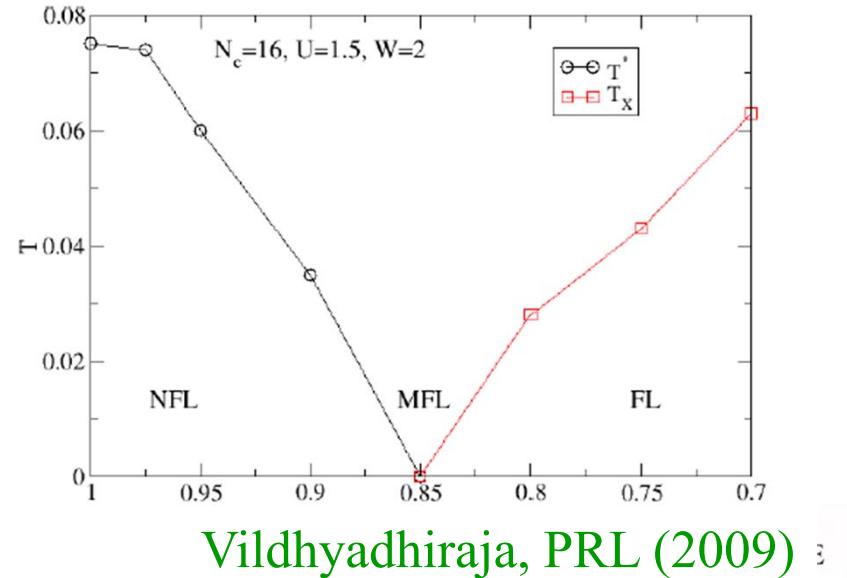
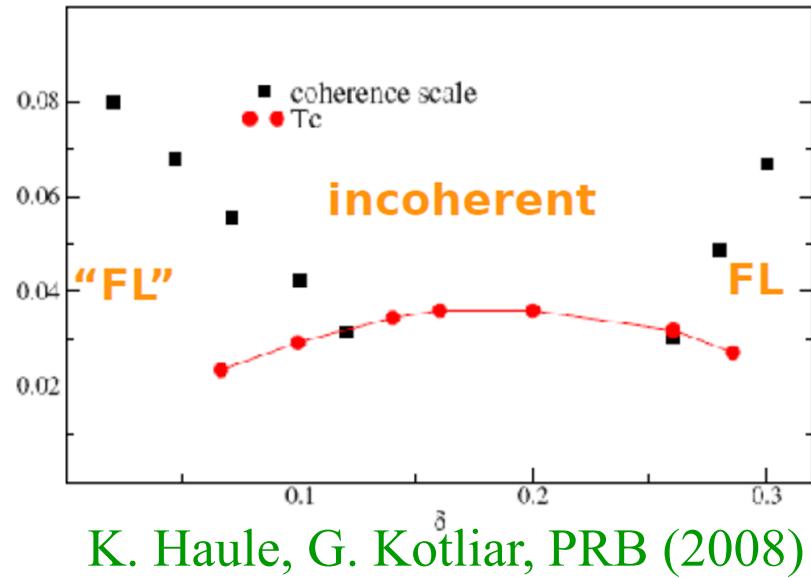
Lesson from DMFT, first order transition + critical  
point governs phase diagram



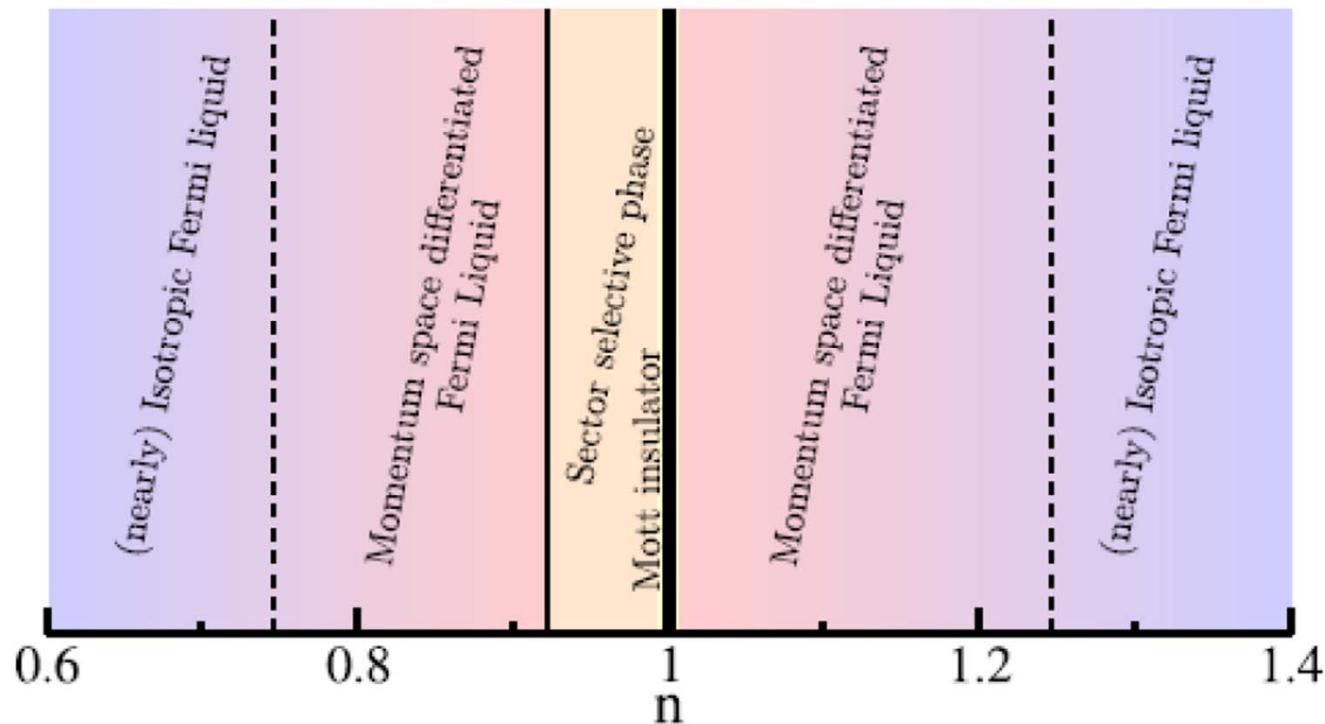
Kristjan Haule

# Doping driven Mott transition, $t' = 0$

Method	$t'$	Orbital selective	$U$	Critical point	Ref.
D+C+H 8			7		Werner et al. cond-mat (2009)
D+C+H 4					Gull et al. EPL (2008)
	-0.3		10,6		Liebsch, Merino... (2008)
					Ferrero et al. PRB (2009)
D+C+H 8			7		Gull, et al. PRB (2009)



# Doping driven Mott transition

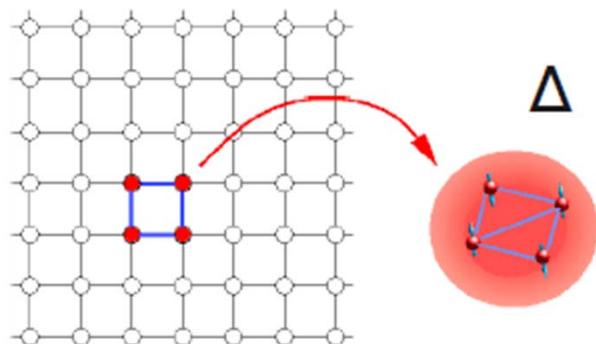


Gull, Werner, Millis, (2009)



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# C-DMFT



Mean-field is not a trivial problem! Many impurity solvers.

Here: continuous time QMC

P. Werner, PRL 2006

P. Werner, PRB 2007

K. Haule, PRB 2007

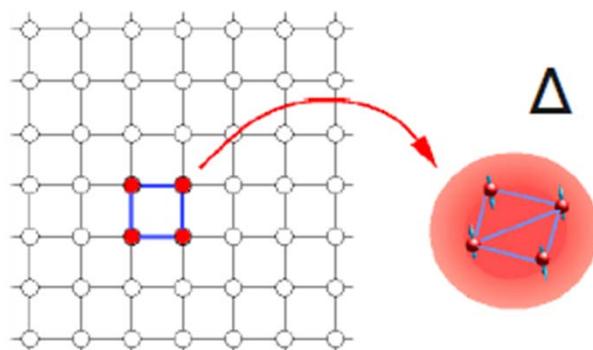
$$Z = \int \mathcal{D}[\psi^\dagger, \psi] e^{-S_c - \int_0^\beta d\tau \int_0^\beta d\tau' \sum_{\mathbf{k}} \psi_{\mathbf{k}}^\dagger(\tau) \Delta(\tau, \tau') \psi_{\mathbf{k}}(\tau')}$$

Continuous-time Quantum Monte Carlo calculations to sum all diagrams generated from expansion in powers of hybridization.

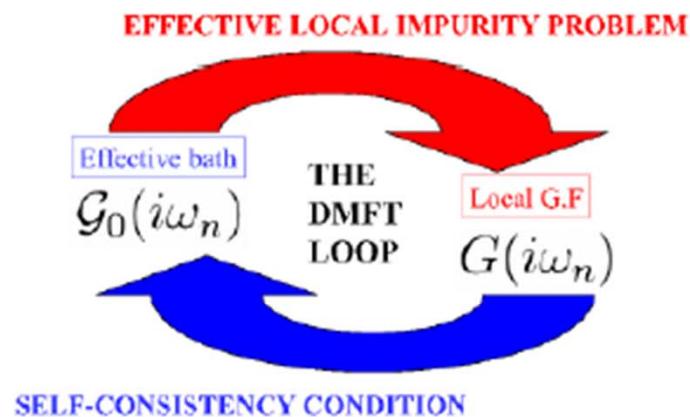
P. Werner, A. Comanac, L. de' Medici, M. Troyer, and A. J. Millis, Phys. Rev. Lett. **97**, 076405 (2006).

K. Haule, Phys. Rev. B **75**, 155113 (2007).

# C-DMFT



$$Z = \int \mathcal{D}[\psi^\dagger, \psi] e^{-S_c - \int_0^\beta d\tau \int_0^\beta d\tau' \sum_{\mathbf{k}} \psi_{\mathbf{k}}^\dagger(\tau) \Delta(\tau, \tau') \psi_{\mathbf{k}}(\tau')}$$



Mean-field is not a trivial problem! Many impurity solvers.

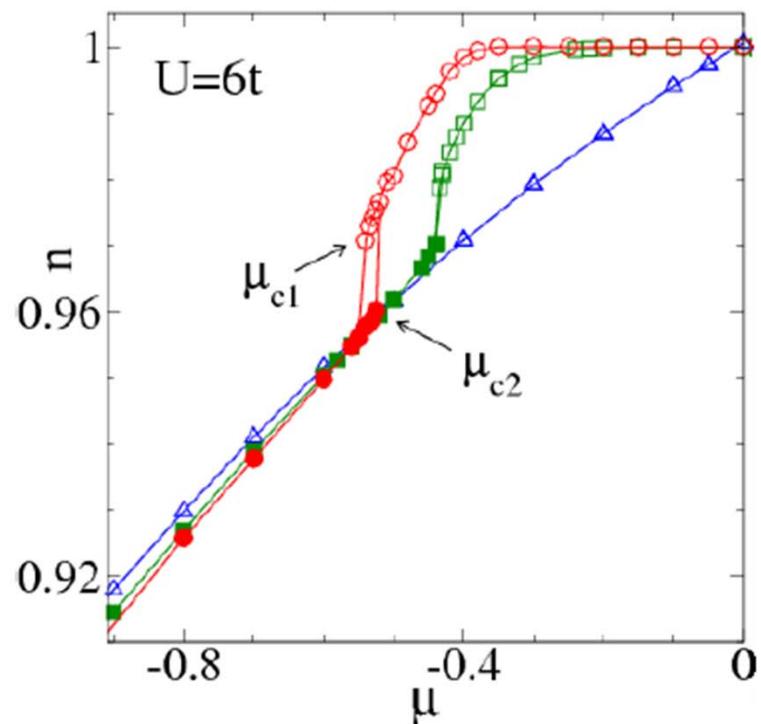
Here: continuous time QMC

- 
- P. Werner, PRL 2006
  - P. Werner, PRB 2007
  - K. Haule, PRB 2007

$$\Delta(i\omega_n) = i\omega_n + \mu - \Sigma_c(i\omega_n)$$

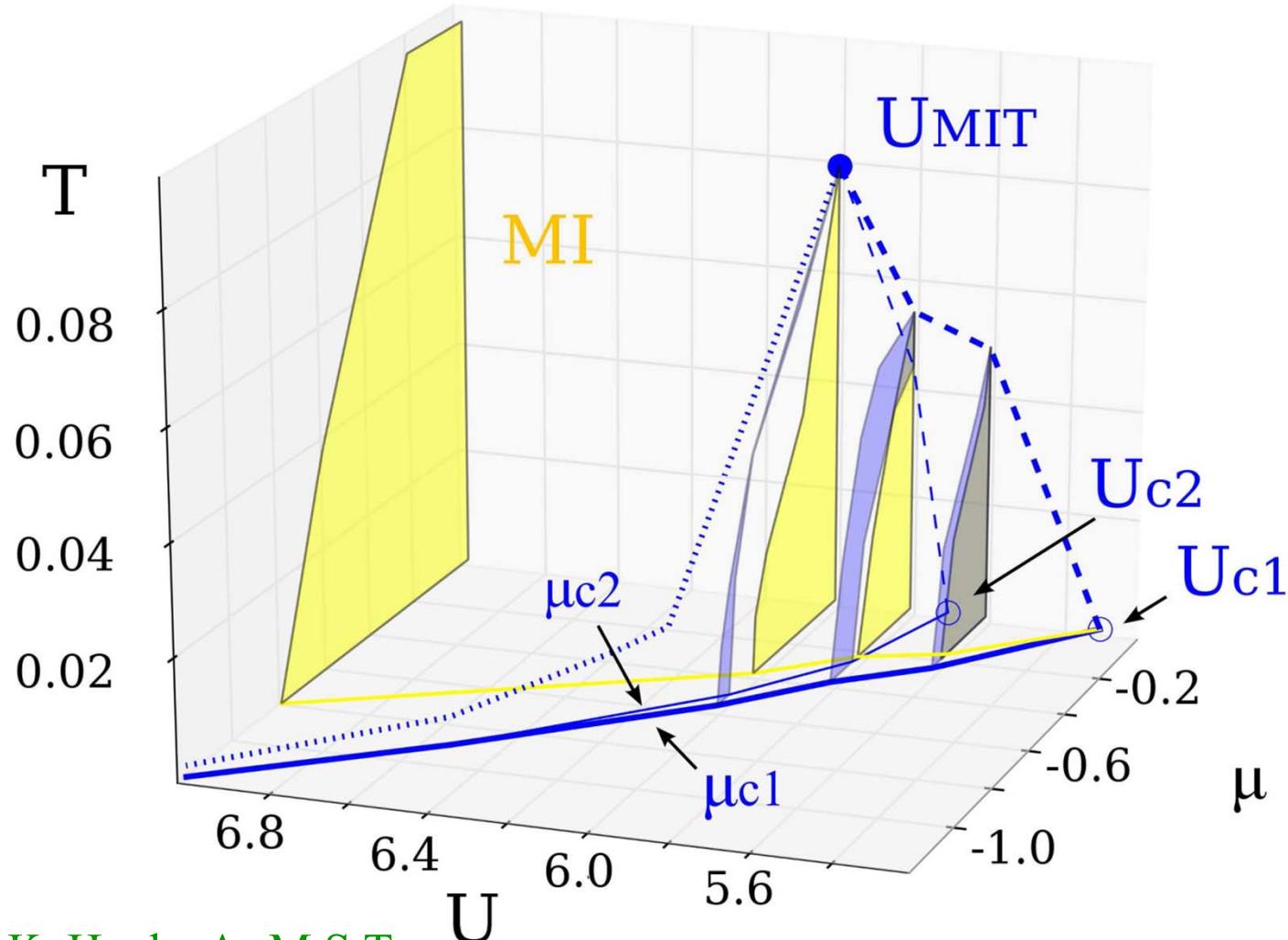
$$- \left[ \sum_{\tilde{k}} \frac{1}{i\omega_n + \mu - t_c(\tilde{k}) - \Sigma_c(i\omega_n)} \right]^{-1}$$

# First order transition at finite doping



$n(\mu)$  for several temperatures:  
 $T/t = 1/10, 1/25, 1/50$

# Normal state phase diagram



G. Sordi, K. Haule, A.-M.S.T  
PRL, 104, 226402 (2010)

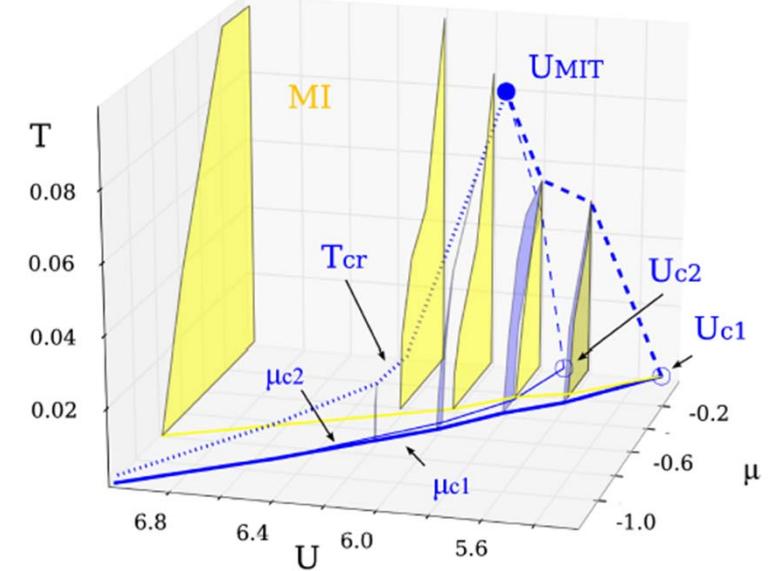
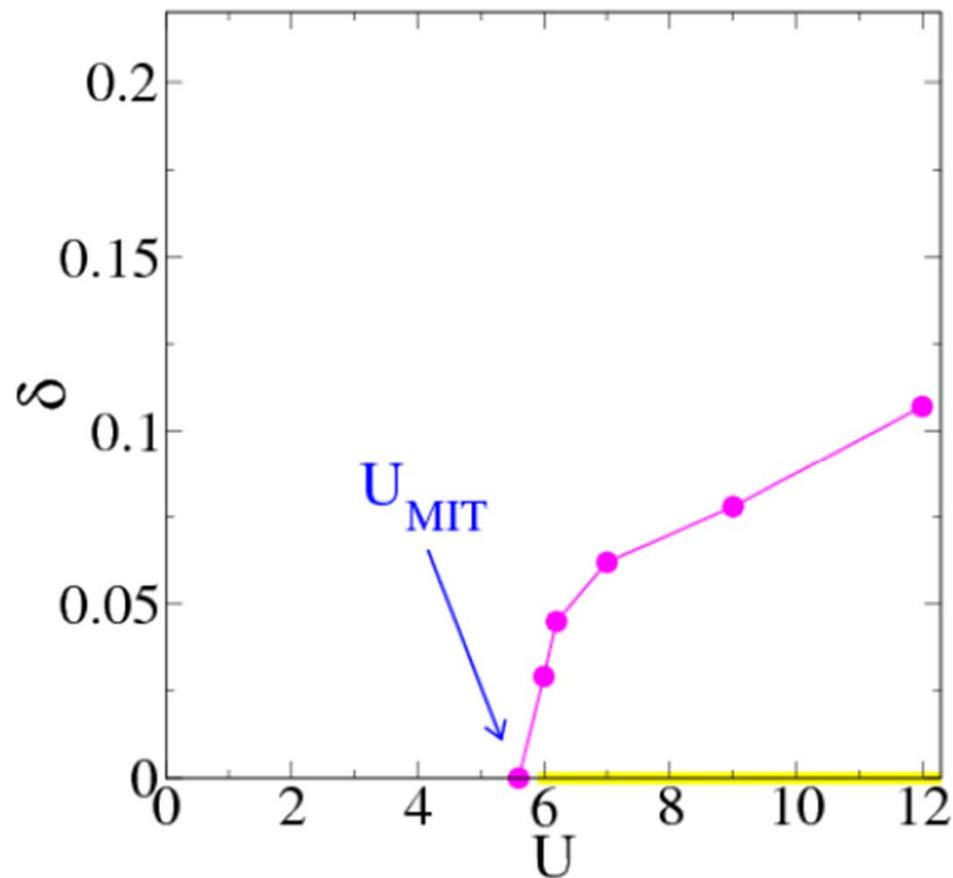
$\mu = 0$ , H. Park, K. Haule, and G. Kotliar,  
Phys. Rev. Lett. 101, 186403 (2008).



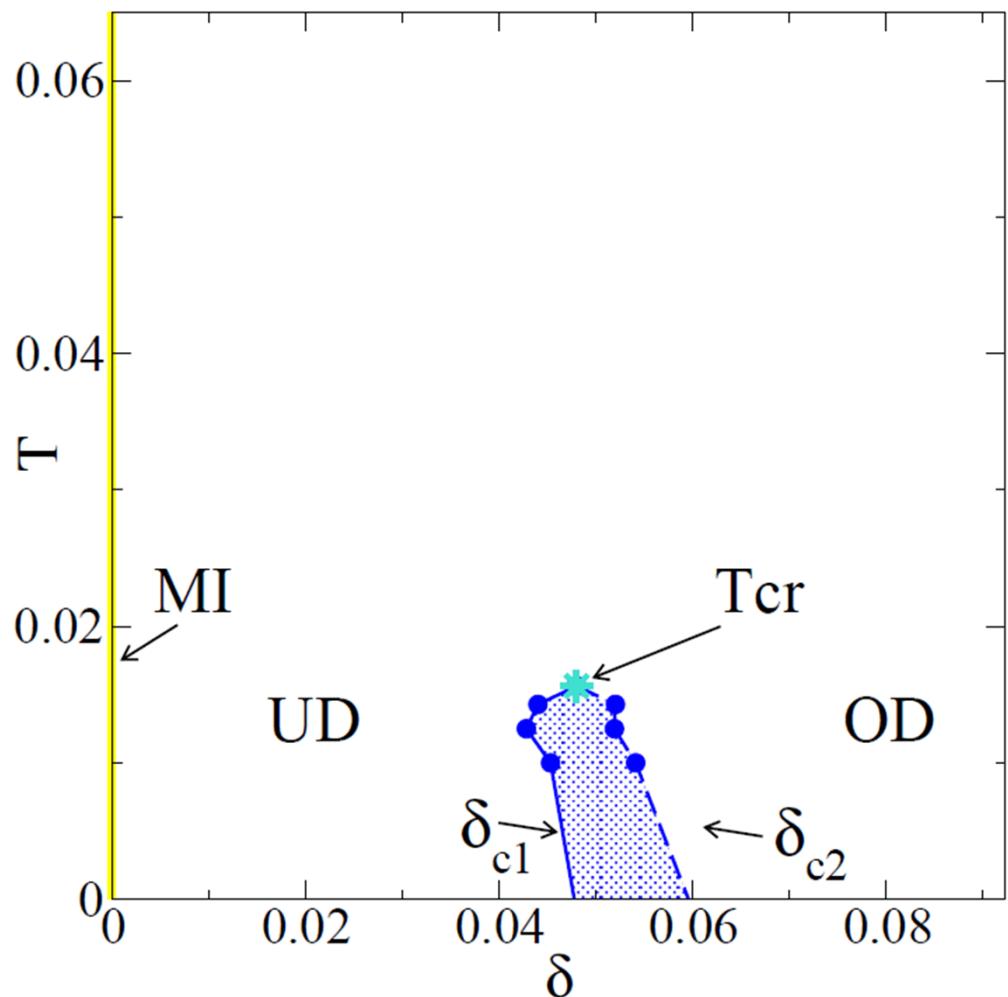
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# Link to Mott transition up to optimal doping

Doping dependence of critical point as a function of  $U$



# Characterisation of the phases ( $U=6.2t$ )



$U > U_{\text{MIT}}$ :

1. Mott insulator (MI)
2. Underdoped phase (UD):  
 $\delta < \delta_c$
3. Overdoped phase (OD):  
 $\delta > \delta_c$
4. Coexistence/forbidden region

Here “optimal doping”  $\delta_c$  = doping at which the 1st order transition occurs

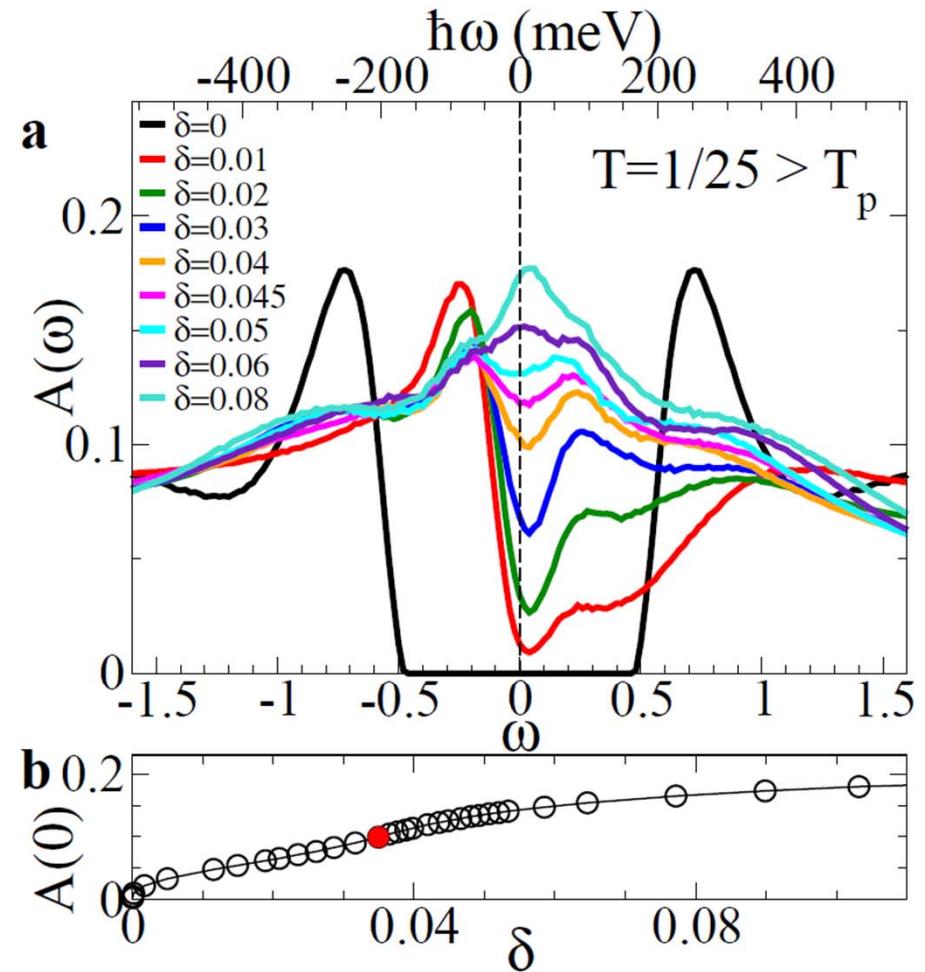
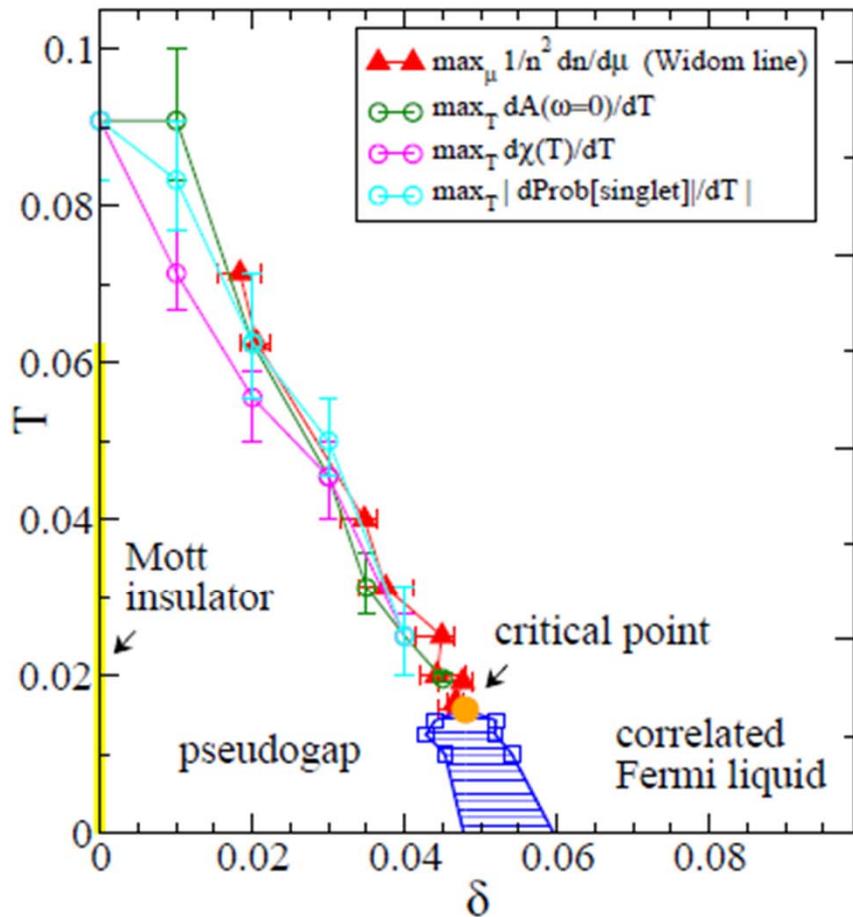
How does the UD phase differ from the OD phase?

Smaller  $D$  and  $S$

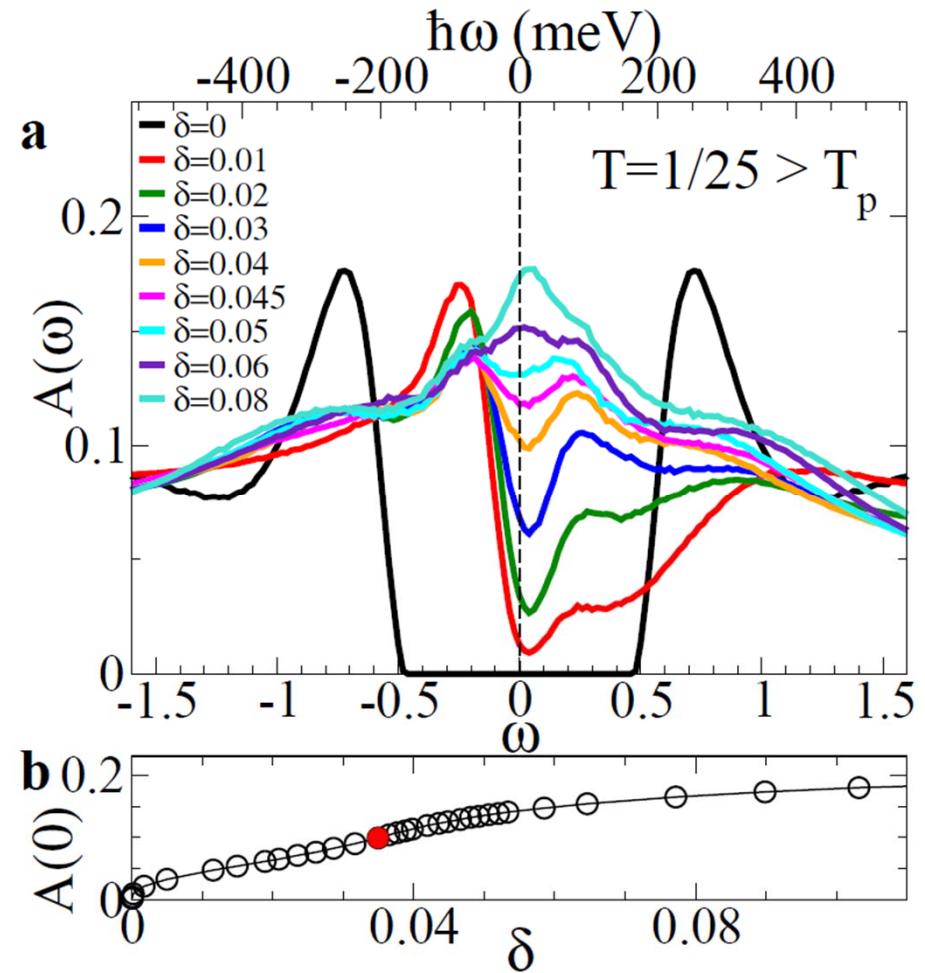
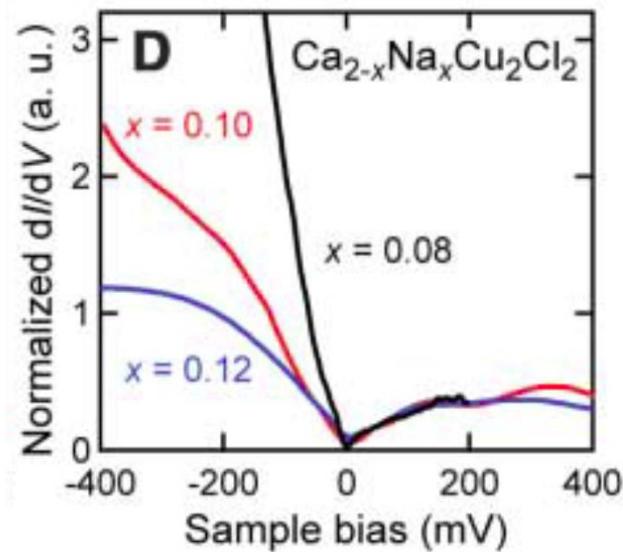


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# Density of states



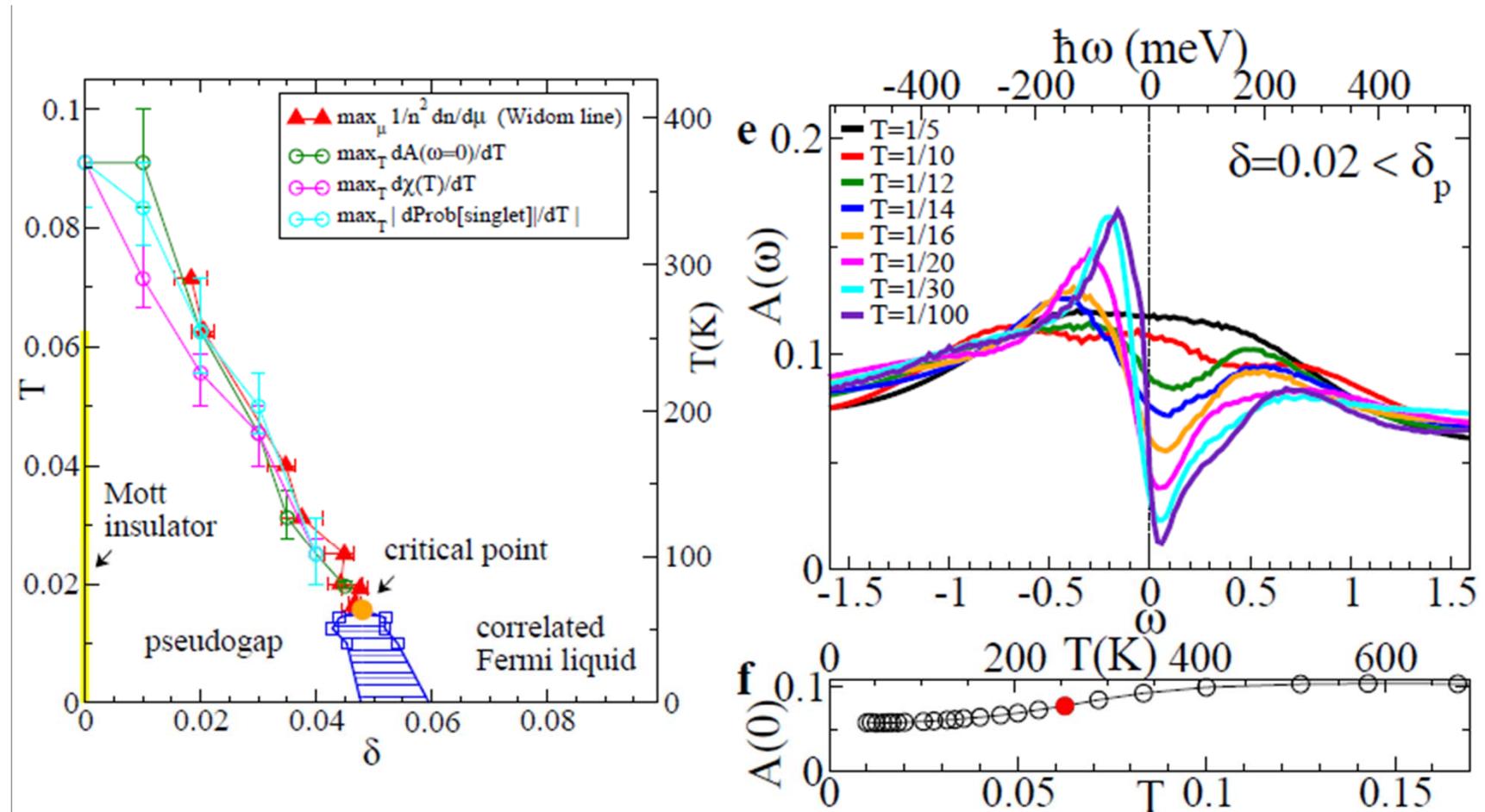
# Density of states



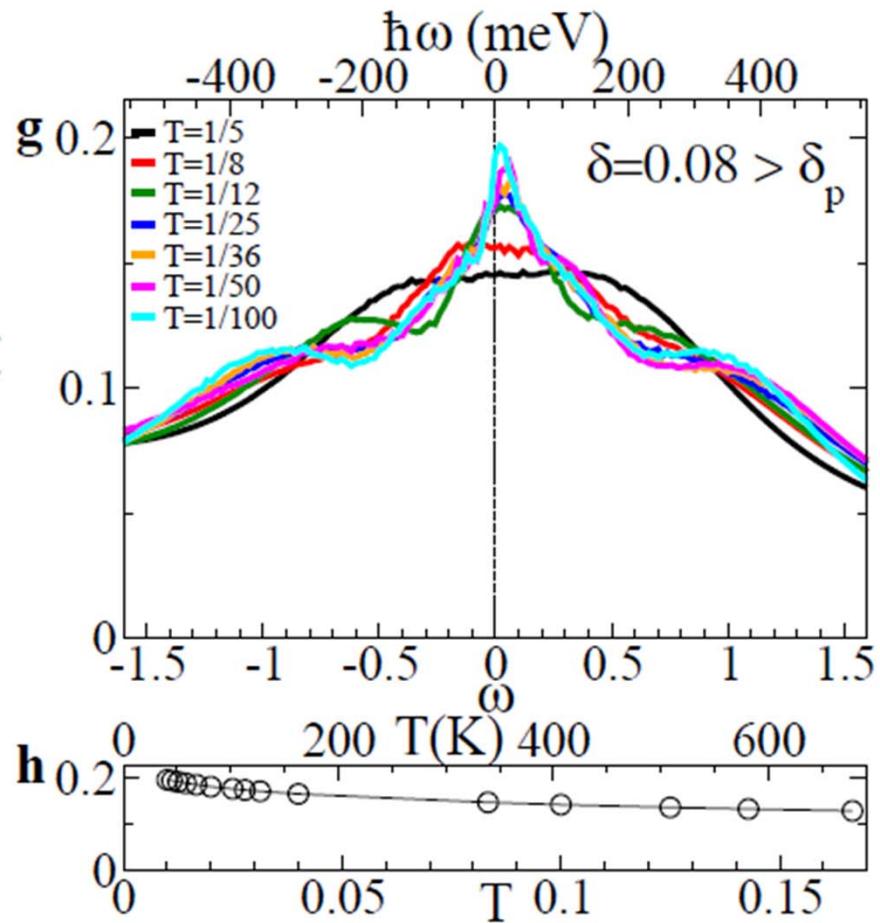
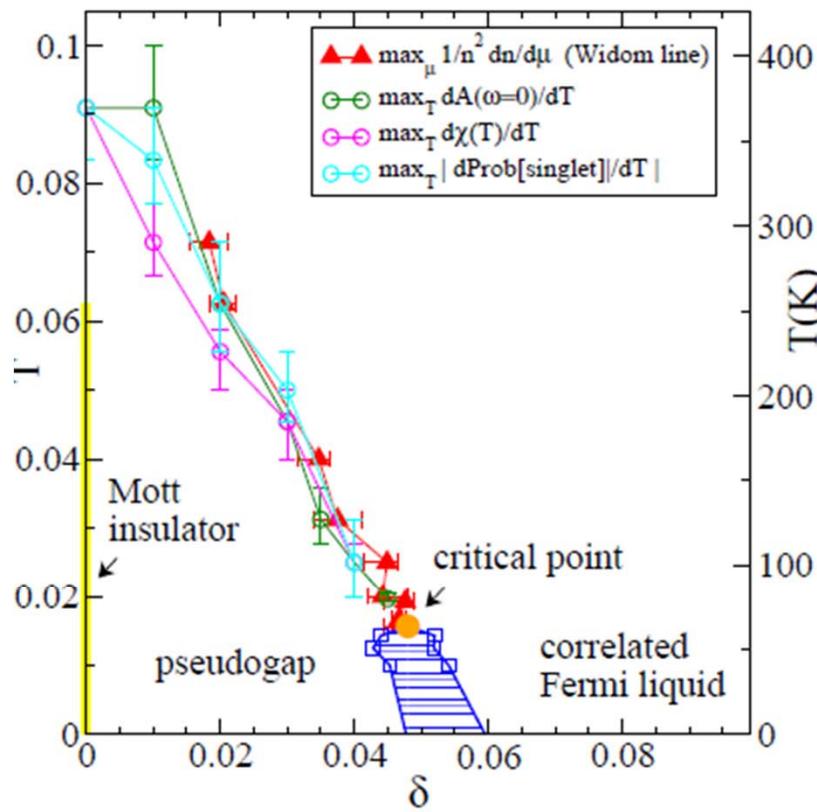
Khosaka et al. *Science* **315**, 1380 (2007);



# Density of states

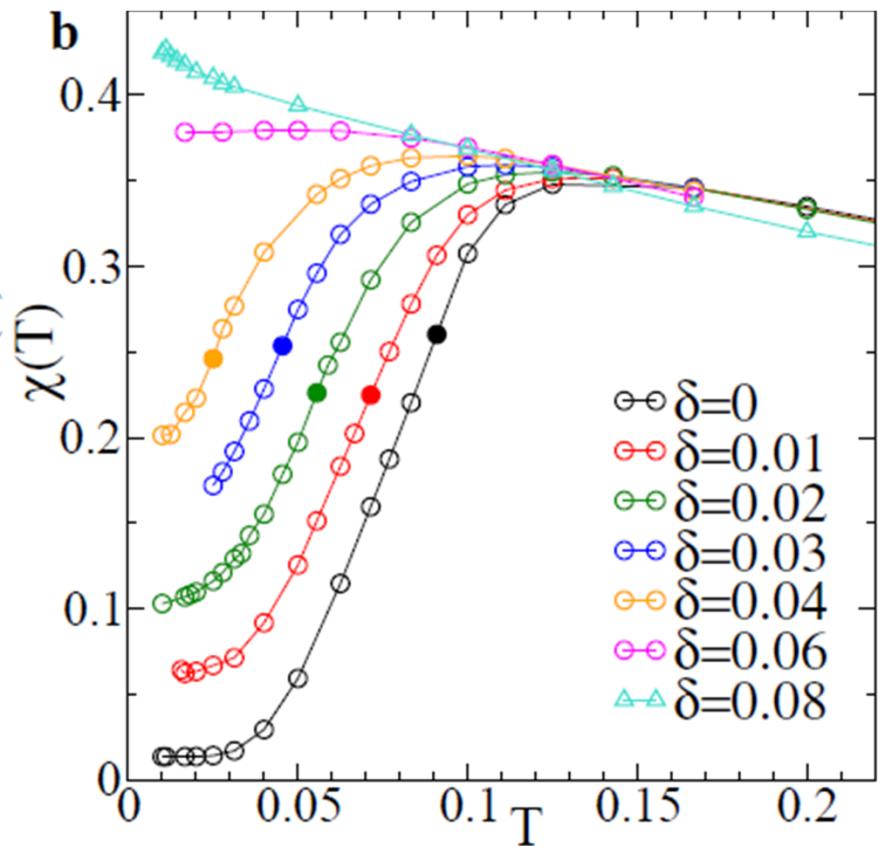
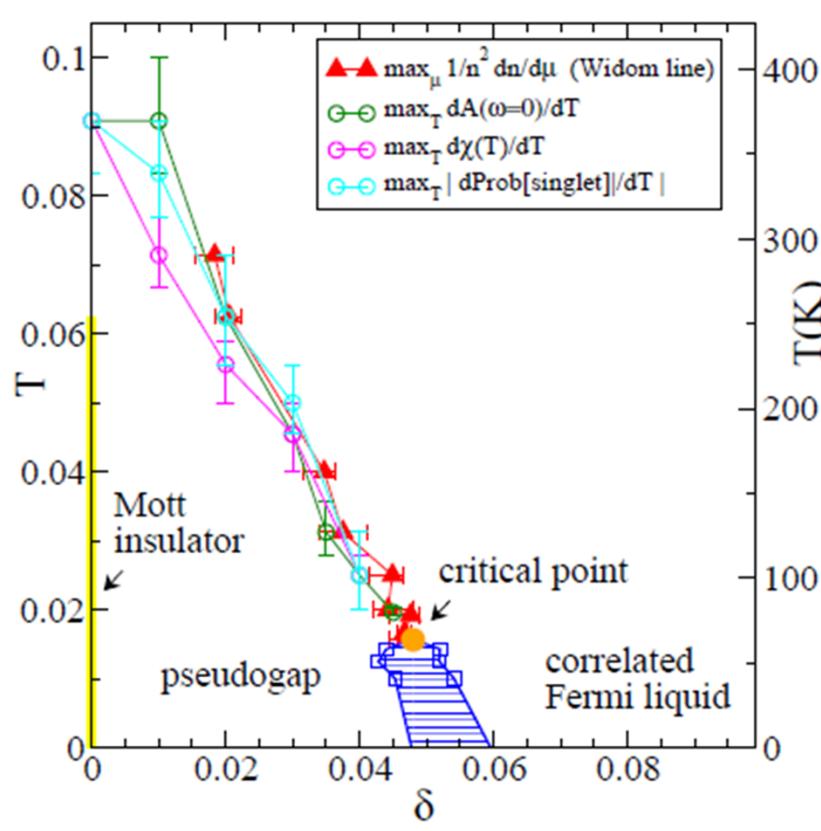


# Density of states

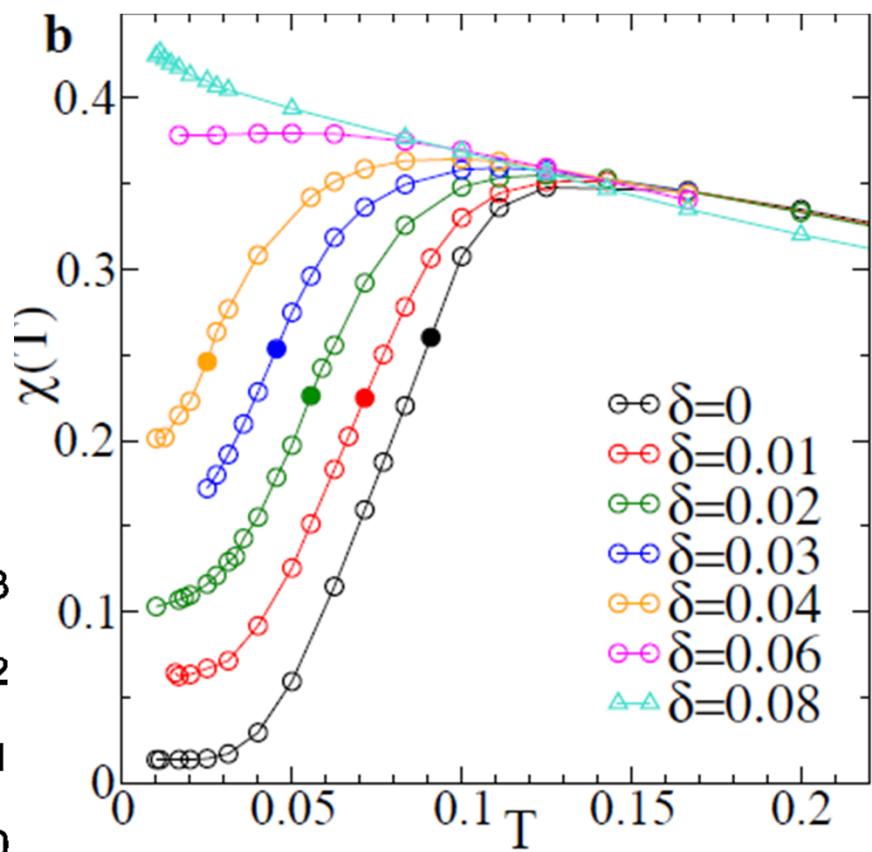
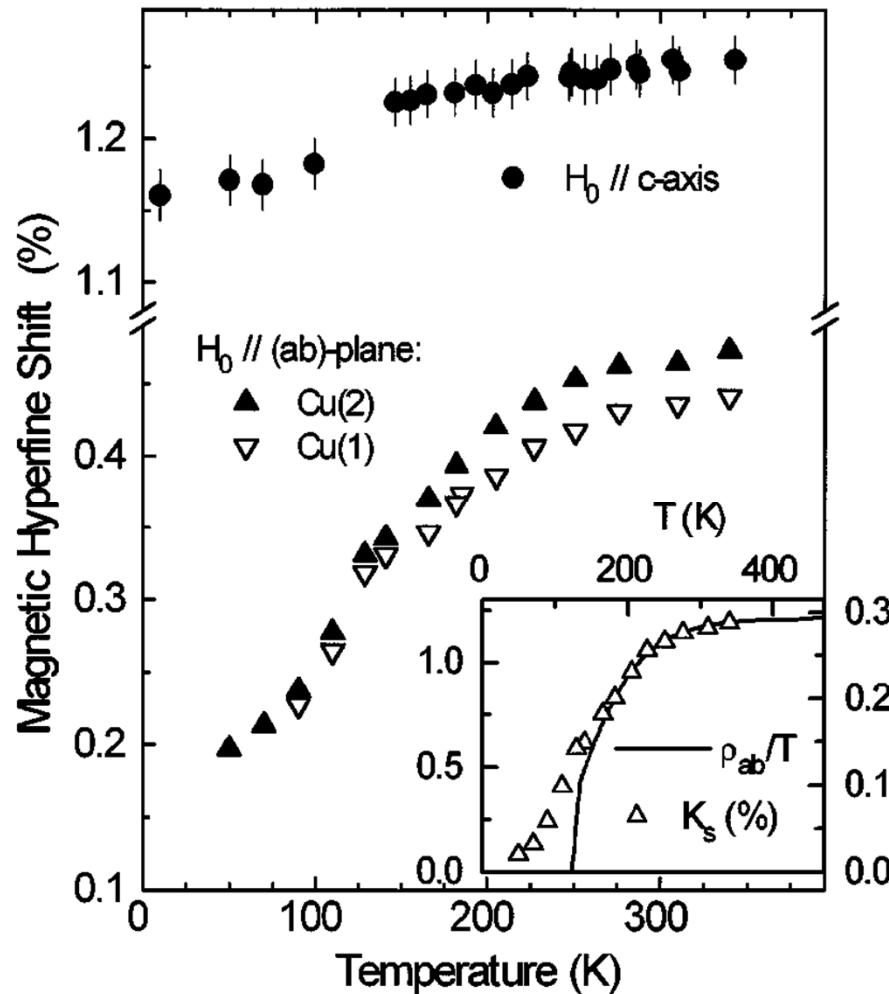


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# Spin susceptibility

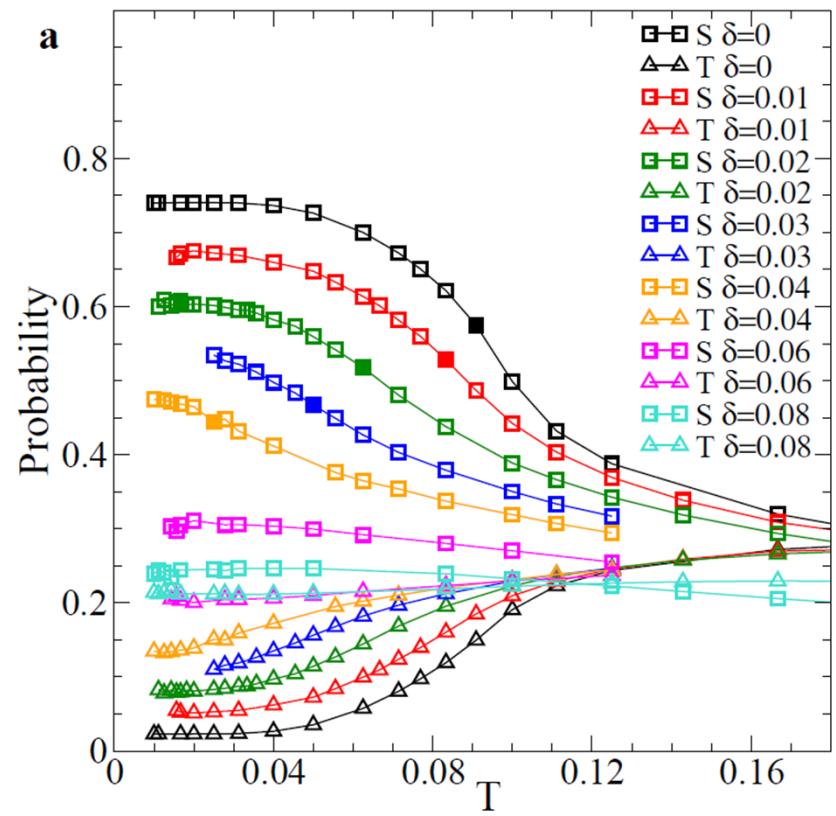
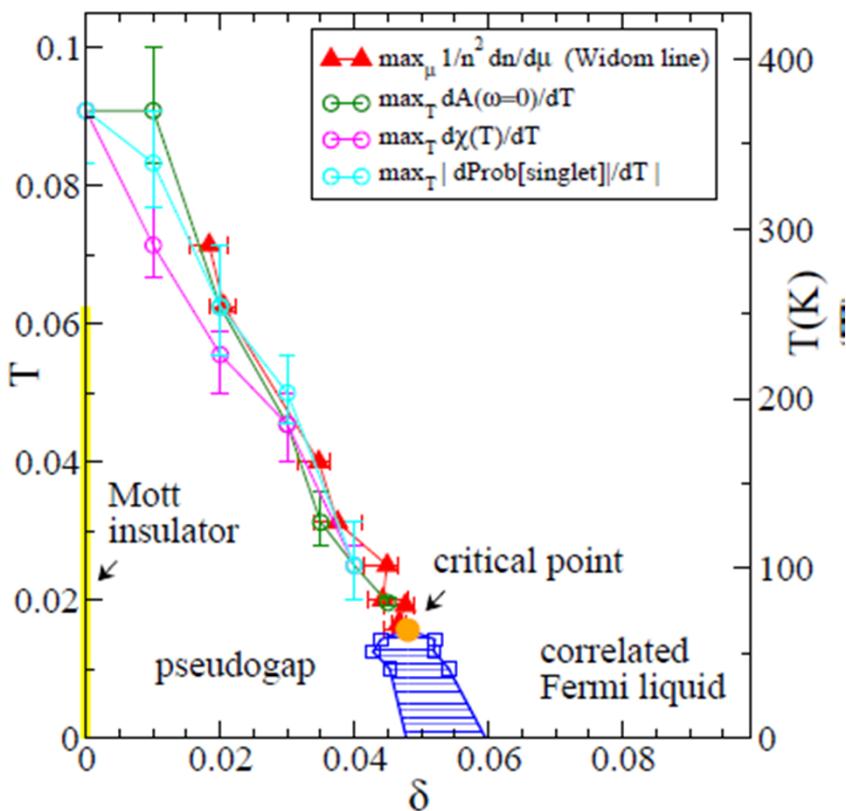


# Spin susceptibility

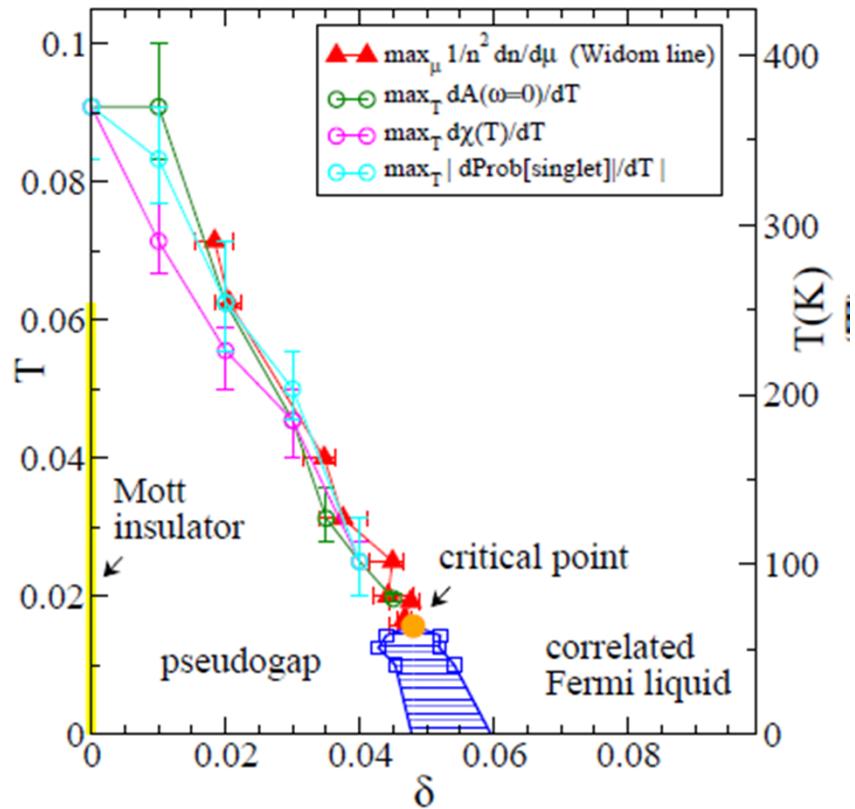


Underdoped Hg1223  
Julien et al. PRL 76, 4238 (1996)

# Plaquette eigenstates



# Pseudogap $T^*$ along the Widom line





Giovanni Sordi



Patrick Sémon



Kristjan Haule

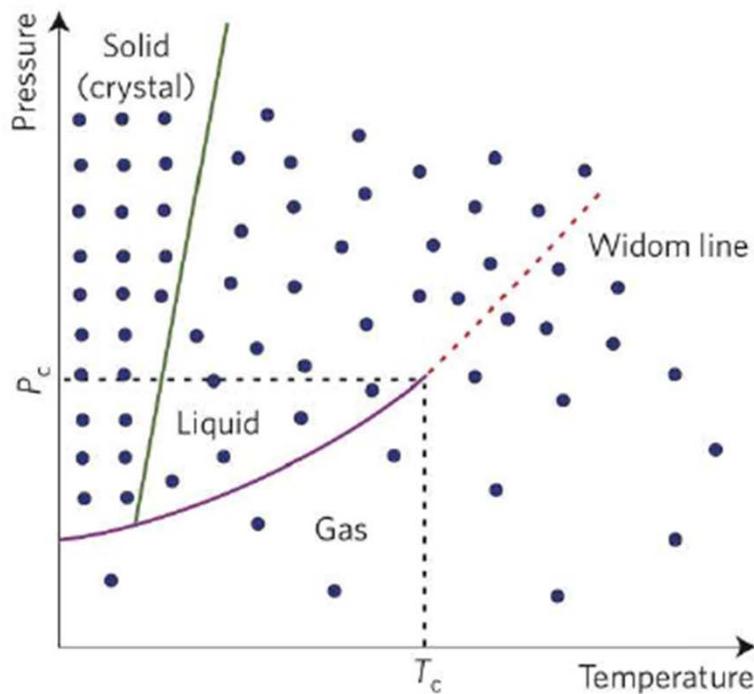
# The Widom line

arXiv:1110.1392



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# What is the Widom line?

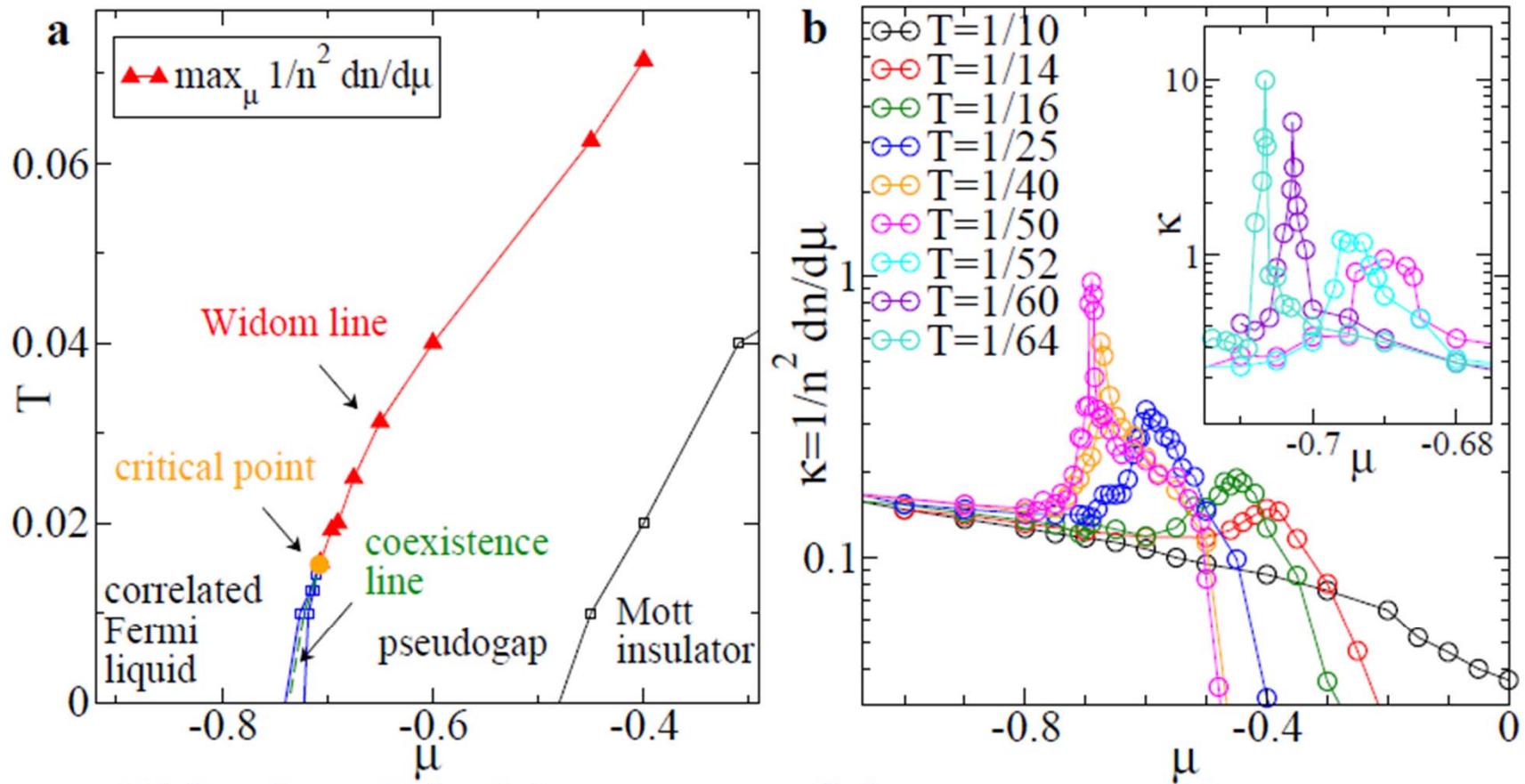


McMillan and Stanley, Nat Phys 2010

- ▶ it is the continuation of the coexistence line in the supercritical region
- ▶ line where the **maxima of different response functions** touch each other asymptotically as  $T \rightarrow T_p$
- ▶ liquid-gas transition in water: max in isobaric heat capacity  $C_p$ , isothermal compressibility, isobaric heat expansion, etc

- ▶ **DYNAMIC crossover arises from crossing the Widom line!**  
water: Xu et al, PNAS 2005,  
Simeoni et al Nat Phys 2010

# Pseudogap $T^*$ along the Widom line



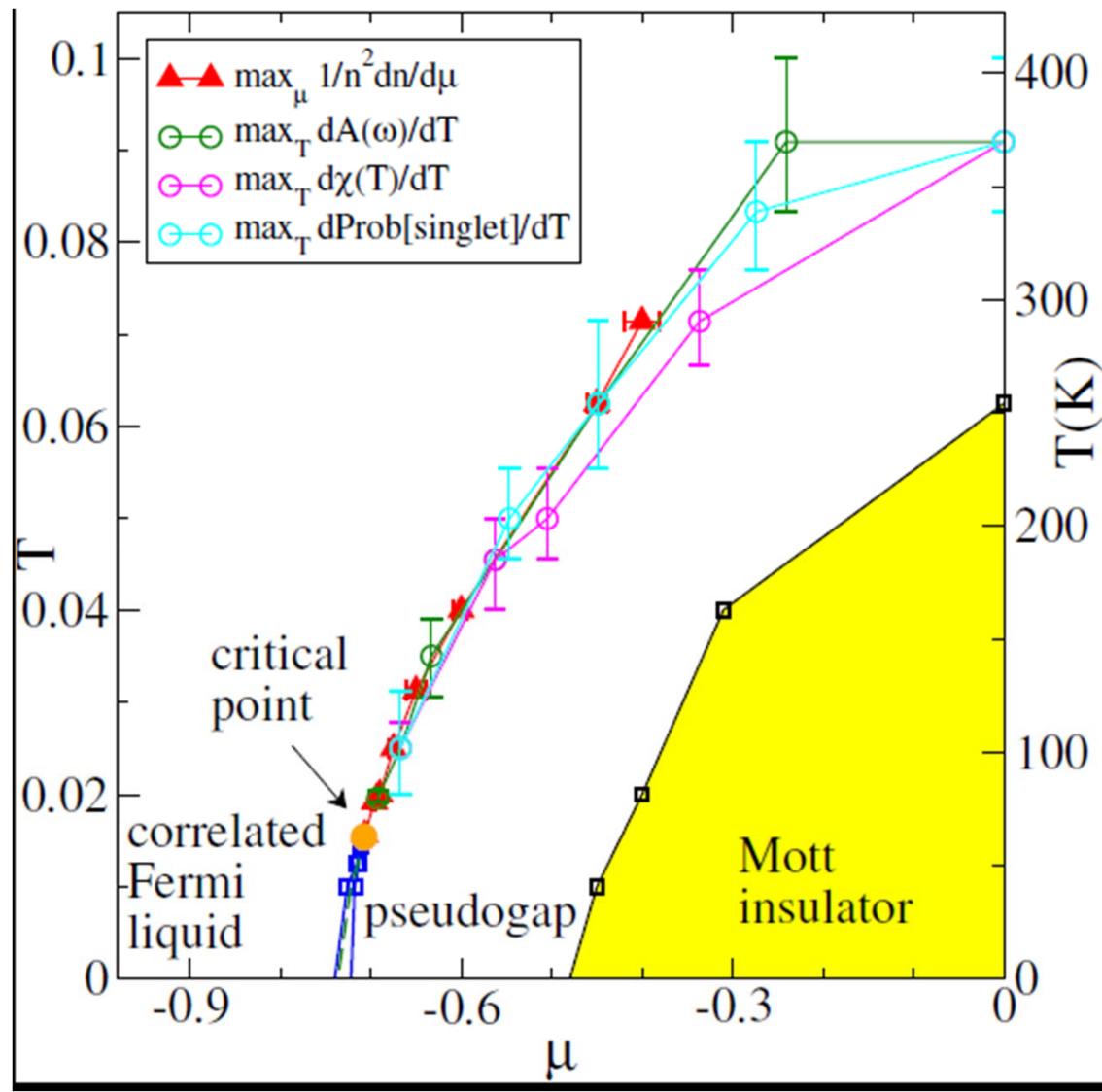
Widom line: defined from maxima of charge compressibility

$$\kappa = 1/n^2(dn/d\mu)_T$$

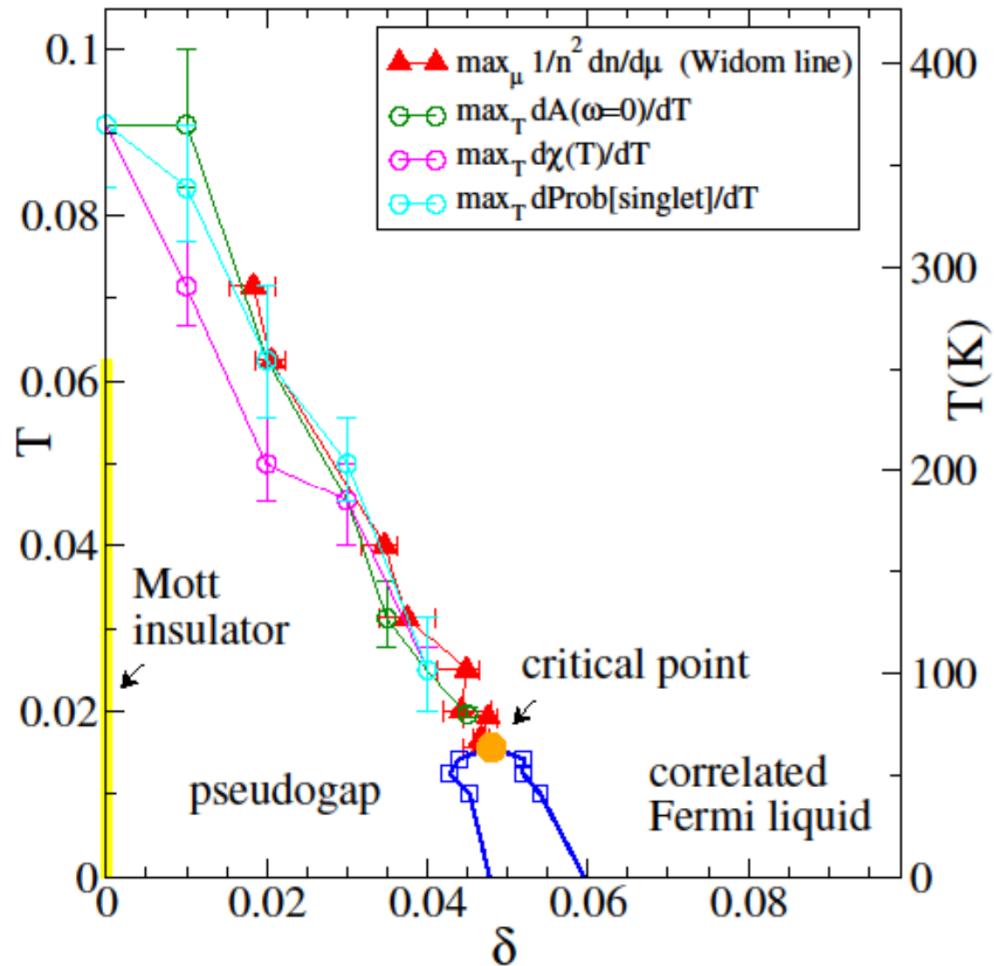
divergence of  $\kappa$  at the (classical) critical point!



# Rapid change also in dynamical quantities

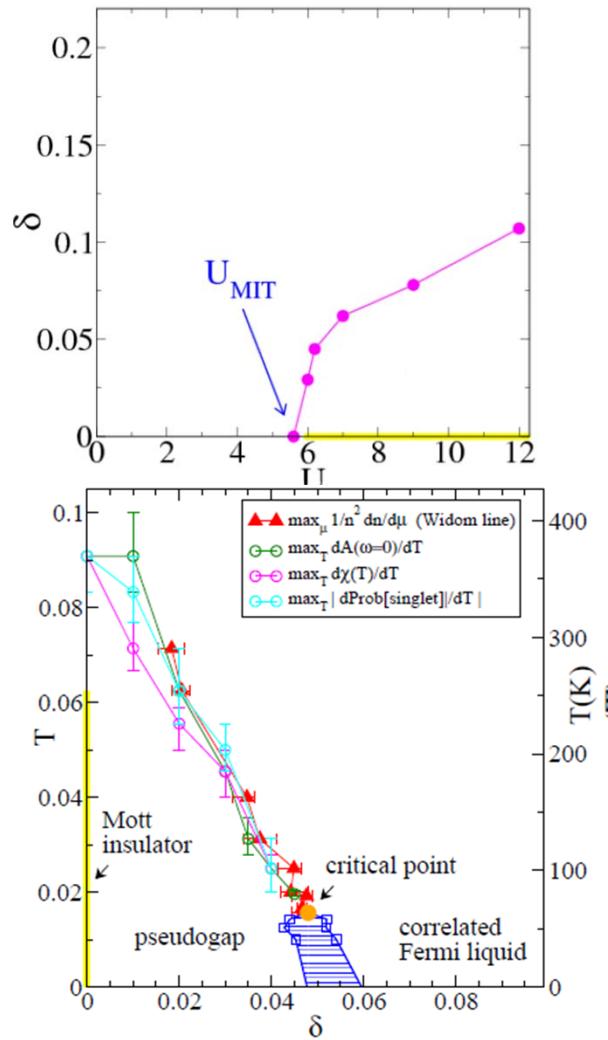


# Phase diagram



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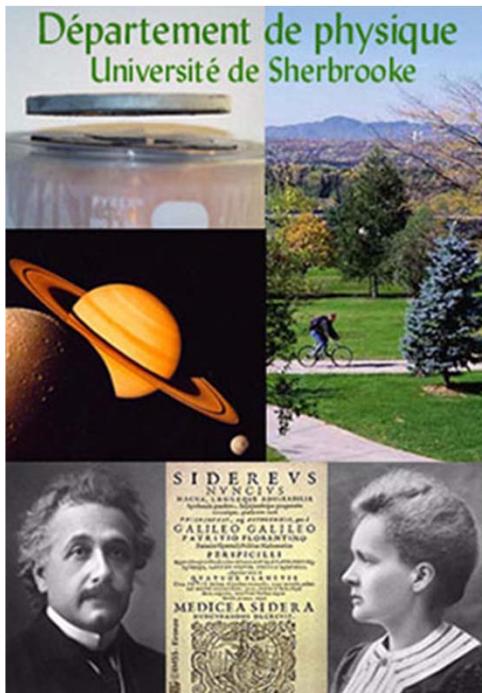
# Summary



- Mott physics extends way beyond half-filling
- Pseudogap is a phase
- Pseudogap  $T^*$  is a Widom line
- High compressibility (stripes?)



# André-Marie Tremblay



Le regroupement québécois sur les matériaux de pointe



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Le calcul de haute performance

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merci

thank you